Safely Filling Gaps with Partial Solutions Common to All Solutions

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Abstract—Gap filling has emerged as a natural sub-problem of many de novo genome assembly projects. The gap filling problem generally asks for an s-t path in an assembly graph whose length matches the gap length estimate. Several methods have addressed it, but only few have focused on strategies for dealing with multiple gap filling solutions and for guaranteeing reliable results. Such strategies include reporting only unique solutions, or exhaustively enumerating all filling solutions and heuristically creating their consensus.

Our main contribution is a new method for reliable gap filling: filling gaps with those sub-paths common to all gap filling solutions. We call these partial solutions safe, following the framework of (Tomescu and Medvedev, RECOMB 2016). We give an efficient safe algorithm running in $O(dm)$ time and space, where $d$ is the gap length estimate and $m$ is the number of edges of the assembly graph. To show the benefits of this method, we implemented this algorithm for the problem of filling gaps in scaffolds. Our experimental results on bacterial and on conservative human assemblies show that, on average, our method can retrieve over 73% more safe and correct bases as compared to previous methods, with a similar precision.

Index Terms—de novo assembly, gap filling, safe solutions, dynamic programming, graph connectivity

1 INTRODUCTION

A common gap filling instance is the reconstruction of the missing sequence between contigs, once their relative order and distance is known from the scaffolding step [1], [9], [14], [21], [23], [29]. Another one is filling the missing sequence between the two reads in a paired-end read [18], [28], [36], [40], [42]. In projects with a known reference, gap filling is applied when assembling novel long insertions in a donor, given length estimates derived from mate-pair alignments to the reference [20].

In the gap filling problem we are given a sequence $X$ containing gaps (e.g. scaffolds produced by a de novo assembler) and a set of sequencing reads. A gap filler aims at filling the gaps in $X$ using the sequencing reads. A natural formulation of the gap filling problem builds an assembly graph of the sequencing reads, and fills a gap by finding an s-t path whose length is consistent with the gap length estimate (here $s$ and $t$ correspond to the two sequences flanking the gap) [25], [26], [40]. (In this paper we allow paths to have repeated vertices.) Since this problem is NP-hard [19], [25], [26], some methods use the heuristic of a shortest s-t path whose length is also consistent with the gap length estimate [15], [40]. Other methods are based on various extension heuristics when navigating the assembly graph from $s$ to $t$ [14], while others patch a gap only with those reads whose pair reliably maps to one of the two sequences flanking the gap [1], [35]. In [25], [26] we showed that the gap filling problem can be solved by dynamic programming in pseudo-polynomial time by an algorithm scaling to real data. On the bacterial and human datasets in the GAGE benchmarks [27], our method can fill in total 76% more gaps with 136% more sequence than previous methods, with a comparable error level.

In this paper we focus on gap fillers that take as input a set of sequences containing gaps and a set of short paired-end or mate-pair sequencing reads. The gap filling problem has also been addressed using preassembled contigs or long reads [7], [13]. Additionally, assembly reconciliation tools such as GAM [3], GAA [41], GAM-NGS [37], and Mix [30] are also able to perform some gap filling, but their aim is rather to merge two or more assemblies into a coherent single assembly.

As new methods filling more gaps and scaling to larger genomes are being developed, the strategies for decreasing the error rate and guaranteeing reliable results become more important. These are even more crucial when considering clinical applications, for example in detecting novel variants in tumors [24]. In Sec. 1.1 we review some reliable gap filling criteria proposed so far in the literature.

In this paper we address the gap filling problem with the “safe and complete” framework proposed in [33] for the contig assembly problem. This framework defines an algorithm for a problem to be: (i) safe, if it returns only partial solutions that are common to all solutions to the problem (these common partial solutions are also called safe), and (ii) complete, if it returns all safe solutions. In terms of the gap filling problem, a safe solution is a path of the assembly graph that is a sub-path of all possible s-t paths whose length matches the gap length estimate. This approach applies to all cases when the entire solution is not unique. For example, in Fig. 1 we show a real assembly graph instance with thousands of possible filling paths, but...
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Fig. 1. Two de Bruijn graphs \((k = 31)\) on staph data corresponding to two gaps in the SGA assembly. They consist of all vertices and edges on an \(s-t\) path of length \(t \in [d−δ,d+δ]\) (graphs \(G_{d,δ}(s,t)\)); notice that these two instances are already acyclic. We represent unary paths by numbers indicating their length. The sub-paths in black are safe i.e., common to all \(s-t\) paths. Top: The gap length estimated by SGA is \(488\), and so we look for paths whose length is approximately \(d + k = 519\) (the path in the de Bruijn graph includes the left and right flanking \(k\)-mers adding \(k\) to the length). The closest value for which there is at least one \(s-t\) path is \(d = 521\). In total there are \(256\) paths with length in the allowed interval. The safe sub-paths have length \(234\) and the precision of Gap2Seq Safe on these sub-paths is \(100\%\). Bottom: The gap length estimated by SGA is \(547\) resulting in a path length estimate of \(578\), but the closest value for which there is at least one \(s-t\) path is \(d = 559\). In total there are \(2304\) paths whose length is in the allowed interval. The safe sub-paths have length \(214\) and the precision of Gap2Seq Safe on these sub-paths is \(100\%\). Notice that most of the bubbles of this graph are caused by single nucleotide mismatches (sequencing errors, SNVs present in the sequenced cell population, or SNV-like differences between different copies of a repeat), because their two parallel unary paths have \(k\) internal nodes.

nevertheless most of the gap is safe. To transform these safe paths into a filling sequence usable in downstream analysis, we fill the gap with an arbitrary filling path, in which we mark the safe and un-safe sub-sequences (e.g., in upper- and lower-case). Fig. 2 shows a simple example.

1.1 Previous work on safe solutions

The safest criteria for having a reliable filling sequence is that the filling path is unique. This strategy is mentioned by Wetzel et al. [40] in connection with \(s-t\) paths whose length matches the gap length estimate. Due to the computational complexity of this latter problem, Wetzel et al. [40] fill a gap with the heuristic criterion of finding a unique shortest \(s-t\) path only. To our knowledge, Konnector [36] is the only method dealing with multiple \(s-t\) paths in a systematic way (Konnector underlies Sealer [21], which is a gap filler of scaffolds). It exhaustively enumerates all \(s-t\) paths in a de Bruijn graph (up to a user defined threshold), and attempts filling a gap only when there are at most a given number of paths (Sealer’s manual recommends 10). It then heuristically computes a multiple alignment of the strings spilled by these paths and takes as filling sequence this consensus sequence (ambiguous positions are encoded with IUPAC codes). Other methods [18] iteratively extend the filling path with a new character if this is well-represented in the consensus of the reads overlapping it.

The idea of this paper originates from a more general research question in bioinformatics about partial solutions common to all solutions. The typical example is the contig assembly problem, where contigs are those strings that are part of all possible genomic reconstructions from an assembly graph (be they Eulerian, Hamiltonian, or just node/edge covering paths)—see e.g., [33]. Another example is the sequence alignment problem, where some studies consider reliable partial alignments [12], [16], [34], or base-pairings common to all optimal or almost-optimal alignments [4], [38]. In the combinatorial optimization community this problem is sometimes called persistency: persistent edges present in all maximum matchings of a bipartite graph [5], or persistent vertices present in all maximum stable sets of a graph [2].

1.2 Contributions of the paper

The main contribution of this paper is a new approach for reliable gap filling based on the notion of safe solution with a strong theoretical foundation.

Second, we propose an efficient safe algorithm for the gap filling problem, running in time \(O(dm)\), where \(d\) is the gap length estimate and \(m\) is the number of edges of the assembly graph. The algorithm is based on finding all sub-paths present in all \(s-t\) paths of an unweighted DAG constructed from the assembly graph. As opposed to [21], [36], this avoids exhaustively enumerating all paths, thus scaling to instances (such as in Fig. 1) with an arbitrary number of paths.

Third, we implement this algorithm as a gap filler of scaffolds. Although this algorithm is not also complete, our experiments on the bacterial assemblies and conservative human assemblies from the GAGE study [27] show that it retrieves, on average, over \(73\%\) more safe and correct bases as compared to previous methods differentiating between ambiguous and unambiguous positions, with a similar precision.

2 METHODS

2.1 Problem definition

In this paper by graph we mean a directed graph. Paths can have repeated vertices, and we will use the term simple path when we need to emphasize that a path does not have repeated vertices. For example, all paths in a directed acyclic graph (DAG) are simple. A path from \(s\) to \(t\) is called an \(s-t\) path. By maximal path satisfying a property \(P\) we mean a path that is not a sub-path of another path satisfying property \(P\). In an edge-weighted graph, the length of a path equals the sum of the weights of its edges.

We re-state below the Exact Path Length problem from [19], with the restriction that the edge lengths are positive.
Problem 1 (Exact Path Length (EPL) with positive weights). Given a directed graph $G = (V, E)$, a weight function $w : E \rightarrow \mathbb{Z}_+$, two vertices $s$ and $t$, and an integer $d$, find an $s$-$t$ path in $G$ of length $d$. In the context of de Bruijn graphs [22] or string graphs [17] for other technical details. The input graph $G$ consists of maximal paths that are sub-paths of all $s$-$t$ paths of the graph $G$.

In [25], [26] we showed that also this restricted version of the problem is NP-complete, by giving a reduction from the Subset Sum problem [8]. Nonetheless, we showed that it can be efficiently solved by dynamic programming in pseudo-polynomial time $O(dm)$, where $m$ is the number of edges of $G$.

We briefly sketch our modeling from [25], [26] of the gap filling problem by the EPL problem, and refer the reader to [25], [26] for other technical details. The input graph can be either a de Bruijn graph [22] or a string graph [17] built on the entire collection of reads. Our implementation uses a de Bruijn graph, in this way, all vertices are labeled by the $k$-mers of the reads and all edges have weight 1. The maximal paths are sub-paths of all these three paths are $(s)$, $(f, g, h)$ and $(b, t)$. Bottom: The gap filling solution is an arbitrary $s$-$t$ path of length $d$, in which these three safe sub-paths are marked (e.g., in upper-case): $S b d F G H T$.

Problem 2 (Safe and complete gap filling). Given a directed graph $G = (V, E)$, a weight function $w : E \rightarrow \mathbb{Z}_+$, two vertices $s$ and $t$, and an integer $d$, find all maximal paths in $G$ that are sub-paths of all $s$-$t$ paths of length $d$. We assume here that the length of each edge of $G$ is 1, otherwise we can subdivide an edge of length $w$ into $w$ edges of length 1 (observe that de Bruijn graphs already satisfy this property). Given $G$, we denote by $G_{d,a}(s, t)$ the graph made up of all the vertices and edges on all $s$-$t$ paths in $G$ of length $\ell \in [d - \delta, d + \delta]$. See Fig. 1 for two graphs $G_{d,\delta}(s, t)$, built on real read data for two gaps in the SGA assembly. The following lemma shows that we can compute $G_{d,\delta}(s, t)$ within the time bound $O(dm)$.

Lemma 1. Given a graph $G = (V, E)$, vertices $s, t \in V$, and distance $d$ and range $\delta = O(d)$, the graph $G_{d,\delta}(s, t)$ can be constructed in time $O(dm)$, where $m = |E|$.

Proof. Let $a(v, \ell)$ equal 1 if there is an $s$-$v$ path of length $\ell \leq d + \delta$, and 0 if no such path exists. Values $a(\cdot, \cdot)$ can be computed in time $O(dm)$ by dynamic programming [25], [26].

Also, for every $i \in \{0, \ldots, d + \delta\}$, let $V_i$ be the set of vertices $v$ of $G$ such that there is an $s$-$v$ path in $G$ of length $i$, and a $v$-$t$ path of length in the interval $[\max(0, d - i - \delta), d - i + \delta]$. It is clear that $V(G_{d,\delta}(s, t)) = \cup_{i=0}^{d+\delta} V_i$.

To construct the sets $V_i$ and the graph $G_{d,\delta}(s, t)$, we initialize $V_{d+i} := \{t\}$ if $a(t, d + \delta) = 1$, otherwise $V_{d+i} := \emptyset$. For the remaining values $i \in \{0, \ldots, d+\delta-1\}$, in decreasing order, we compute $V_i$ as follows.

If $i \in [d - \delta, d + \delta]$ and $a(t, i) = 1$, then initialize as above $V_i := \{t\}$, otherwise $V_i := \emptyset$. To $V_i$ we add all in-neighbors $v$ of the vertices of $V_{i+1}$ for which $a(v, i) = 1$. During this computation we can also extract all edges from such vertices $v$ to vertices in $V_{i+1}$.

There are $d+\delta+1$ sets $V_i$, thus each edge of $G$ is inspected at most $O(d)$ times. Thus, the complexity of computing $G_{d,\delta}(s, t)$ is $O(dm)$. \qed

Problem 3 (Safe and complete gap filling – extended). Given a directed graph $G = (V, E)$, a weight function $w : E \rightarrow \mathbb{Z}_+$, two vertices $s$ and $t$, and integers $d, \delta$, find all maximal paths in $G$ that are sub-paths of all $s$-$t$ paths of length in the interval $[d - \delta, d + \delta]$. Clearly, Problem 3 generalizes Problem 2 when taking $\delta = 0$. Moreover, to simplify our complexity bounds, we will assume throughout this paper that $\delta = O(d)$.

We leave open the existence of an (efficient) algorithm for these two safe and complete gap filling problems (Problems 2 and 3). However, in the next section we propose an efficient safe algorithm for them. We will show experimentally, in Sec. 4, that this algorithm applied to Problem 3 has very good performance both in terms of running time and amount of safe paths that it retrieves.

2.2 A safe algorithm based on paths common to all $s$-$t$ paths in a DAG

We assume here that the length of each edge of $G$ is 1, otherwise we can subdivide an edge of length $w$ into $w$ edges of length 1 (observe that de Bruijn graphs already satisfy this property). Given $G$, we denote by $G_{d,\delta}(s, t)$ the graph made up of all the vertices and edges on all $s$-$t$ paths in $G$ of length $\ell \in [d - \delta, d + \delta]$. See Fig. 1 for two graphs $G_{d,\delta}(s, t)$, built on real read data for two gaps in the SGA assembly. The following lemma shows that we can compute $G_{d,\delta}(s, t)$ within the time bound $O(dm)$.

Lemma 1. Given a graph $G = (V, E)$, vertices $s, t \in V$, and distance $d$ and range $\delta = O(d)$, the graph $G_{d,\delta}(s, t)$ can be constructed in time $O(dm)$, where $m = |E|$.

Proof. Let $a(v, \ell)$ equal 1 if there is an $s$-$v$ path of length $\ell \leq d + \delta$, and 0 if no such path exists. Values $a(\cdot, \cdot)$ can be computed in time $O(dm)$ by dynamic programming [25], [26].

Also, for every $i \in \{0, \ldots, d + \delta\}$, let $V_i$ be the set of vertices $v$ of $G$ such that there is an $s$-$v$ path in $G$ of length $i$, and a $v$-$t$ path of length in the interval $[\max(0, d - i - \delta), d - i + \delta]$. It is clear that $V(G_{d,\delta}(s, t)) = \cup_{i=0}^{d+\delta} V_i$.

To construct the sets $V_i$ and the graph $G_{d,\delta}(s, t)$, we initialize $V_{d+i} := \{t\}$ if $a(t, d + \delta) = 1$, otherwise $V_{d+i} := \emptyset$. For the remaining values $i \in \{0, \ldots, d+\delta-1\}$, in decreasing order, we compute $V_i$ as follows.

If $i \in [d - \delta, d + \delta]$ and $a(t, i) = 1$, then initialize as above $V_i := \{t\}$, otherwise $V_i := \emptyset$. To $V_i$ we add all in-neighbors $v$ of the vertices of $V_{i+1}$ for which $a(v, i) = 1$. During this computation we can also extract all edges from such vertices $v$ to vertices in $V_{i+1}$.

There are $d+\delta+1$ sets $V_i$, thus each edge of $G$ is inspected at most $O(d)$ times. Thus, the complexity of computing $G_{d,\delta}(s, t)$ is $O(dm)$. \qed

Given $G_{d,\delta}(s, t)$, we compute the graph $G_{d,\delta}^{SCC}(s, t)$ of strongly connected components of $G_{d,\delta}(s, t)$. The graph $G_{d,\delta}^{SCC}(s, t)$ is usually defined to have as vertices, sets of vertices of $G_{d,\delta}(s, t)$, i.e., its strongly connected components. However, to simplify notation, if a strongly connected component of $G_{d,\delta}(s, t)$ consists of a single vertex $v$, we consider that the corresponding vertex of $G_{d,\delta}^{SCC}(s, t)$ is $v$, instead of $\{v\}$. Such strongly connected component will be called
Lemma 2. Let \( P \) be a path in \( G^{SCC}_{d,\delta}(s,t) \) that is a sub-path of all \( s,t \) paths in \( G^{SCC}_{d,\delta}(s,t) \), and let \( Q \) be a sub-path of \( P \) made up of only vertices corresponding to trivial strongly connected components of \( G_{d,\delta}(s,t) \). Then \( Q \) is a sub-path of all \( s,t \) paths of \( G_{d,\delta}(s,t) \) of length in the interval \([d-\delta, d+\delta]\).

Proof. It is enough to show that \( Q \) is a sub-path of all \( s,t \) paths of \( G_{d,\delta}(s,t) \), since among the \( s,t \) paths of \( G_{d,\delta}(s,t) \) there are also all those of all lengths in \([d-\delta, d+\delta]\). To show this, let \( R \) be an arbitrary \( s,t \) path in \( G_{d,\delta}(s,t) \). Let \( R^{SCC} \) be the path in \( G^{SCC}(s,t) \) made up of those strongly connected components whose vertices are used by \( R \) (observe that \( R^{SCC} \) is indeed an \( s,t \) path in \( G^{SCC}_{d,\delta}(s,t) \)). By the assumption on \( P \), we have that \( P \) is a sub-path of \( R^{SCC} \). By transitivity, it follows that also \( Q \) is a sub-path of \( R^{SCC} \). Since \( Q \) is made up of only vertices corresponding to trivially strongly connected components of \( G_{d,\delta}(s,t) \), we get that \( Q \) is a sub-path of \( R \).

Let \( H^U \) be the undirected graph underlying \( H \). Recall that a bridge in \( H^U \) is an edge whose removal makes \( H^U \) disconnected, and a cut vertex is a vertex whose removal makes \( H^U \) disconnected. We now prove that an edge \( e \) appears on all \( s,t \) paths of \( H \) if and only if the corresponding undirected edge \( e^U \) of \( H^U \) is a bridge.

\((\Rightarrow)\) Suppose that \( e \) appears on all \( s,t \) paths of \( H \). Since \( s \) is a source and \( t \) is a sink, then any undirected \( s,t \) path in \( H^U \) must be directed from \( s \) to \( t \) in \( H \). Therefore, \( e^U \) also belongs to all undirected \( s,t \) simple paths in \( H^U \). Therefore, removing \( e^U \) disconnects \( s \) and \( t \), and thus \( H \). Therefore, \( e^U \) is a bridge.

\((\Leftarrow)\) Let \( e \) be an edge of \( H \) and suppose that the undirected edge \( e^U \) of \( H^U \) is a bridge. Suppose for a contradiction that there is an \( s,t \) path \( P \) in \( H \) on which \( e \) does not appear, and let \( P^U \) be the corresponding undirected path in \( H^U \). In any DAG with a unique source \( s \) and a unique sink \( t \) for every vertex \( v \) there is an \( s,v \) path \( P_v \) and a \( v,t \) path \( Q_v \). Let \( P^U_v \) and \( Q^U_v \) be the corresponding undirected \( s,v \) and \( v,t \) paths in \( H^U \). By removing \( e^U \) from \( H^U \), at least one of \( P^U_v \) or \( Q^U_v \) still remains in \( H^U \) (i.e., \( e^U \)), for every vertex \( v \). Moreover, \( P^U \) is still a path of \( H^U \) (i.e., \( e^U \)), since \( e \) does not appear on \( P \). In summary, from every vertex \( v \) there is a path in \( H^U \) (i.e., \( e^U \)) to either \( s \) or \( t \), and \( s \) and \( t \) are connected by a path in \( H^U \) (i.e., \( e^U \)). Thus, \( H^U \) is connected, which contradicts the fact that \( e^U \) is a bridge of \( H^U \).

In an entirely analogous manner we can prove that a vertex \( v \) appears on all \( s,t \) paths of \( H \) if and only if \( v \) is a cut vertex of \( H^U \). All bridges and cut vertices of \( H^U \) can be found in time \( O(m) \) using Tarjan’s algorithms [11], [32], which gives the desired result.

The safe algorithm for the gap filling problem, running in time \( O(dm) \), is summarized in Algorithm 1. It starts by computing the graph \( G_{d,\delta}(s,t) \) made up of all the vertices and edges of \( G \) on all \( s,t \) paths of all lengths \( \ell \in [d-\delta, d+\delta] \). It then considers its graph \( G^{SCC}_{d,\delta}(s,t) \) of strongly connected components, and finds, using Theorem 1, all paths of \( G^{SCC}_{d,\delta}(s,t) \) common to all \( s,t \) paths of \( G_{d,\delta}(s,t) \). By Lemma 2 we know that these paths are safe for the gap filling problem.

3 IMPLEMENTATIONS

We implemented the algorithm described in Sec. 2.2 as version 2.1 of Gap2Seq [25], [26], which is our tool for filling gaps in scaffolds.

Gap2Seq v1.0 [25], [26] builds a de Bruijn graph of order \( k \) from all the reads, in which all \( k \)-mers have abundance at least \( r \), using GATB [6]. We used the default values (\( k = 31 \) and \( r = 2 \)) on the bacterial data sets and \( k = 61 \) and \( r = 2 \) on the human chromosome 14 data. For each gap, it locates in the de Bruijn graph the last \( e \) \( k \)-mers (default \( e = 10 \)) of the left flanking contig (and adds \( s \) as in-neighbor of these vertices), and the first \( e \) \( k \)-mers of the right flanking contig (and adds \( t \) as out-neighbor of these vertices). It then computes the values \( a(v, \ell) \) equalling 1 if there is an \( s,v \) path of length \( \ell \), and 0 if no such path exists (recall proof of Lemma 1).

It then finds the value \( d' \) that is closest to the estimated gap length (i.e., marked by N’s inside the scaffold) and for
Algorithm 1: An efficient safe algorithm for the gap filling problem.

**INPUT:** A directed graph $G$, two vertices $s$ and $t$, a length $d$ and a range $\delta$.

**OUTPUT:** An $s$-$t$ path of length $\ell \in [d - \delta, d + \delta]$ in $G$ with some vertices and edges belonging to all $s$-$t$ of all lengths $\ell \in [d - \delta, d + \delta]$ marked.

1. compute $G_{d,\delta}(s,t)$; (by Lemma 1)
   - all $s$-$t$ paths of length $\ell \in [d - \delta, d + \delta]$ in $G$ are also $s$-$t$ paths of length $\ell$ in $G_{d,\delta}(s,t)$, but $G_{d,\delta}(s,t)$ may also have other $s$-$t$ paths;
2. compute $G_{d,\delta}^{SCC}(s,t)$; (using [31])
   - Lemma 2 tells how sub-paths of all $s$-$t$ paths of $G_{d,\delta}^{SCC}(s,t)$ induce sub-paths of all $s$-$t$ paths of all lengths $\ell \in [d - \delta, d + \delta]$ in $G$;
   - To find all sub-paths of all $s$-$t$ paths of $G_{d,\delta}^{SCC}(s,t)$ we apply the proof of Theorem 1, as follows:
3. compute the set $B$ of bridges of the undirected graph underlying $G_{d,\delta}^{SCC}(s,t)$; (using [32])
4. compute the set $C$ of cut vertices of the undirected graph underlying $G_{d,\delta}^{SCC}(s,t)$; (using [11])
5. find one $s$-$t$ path $P$ in $G$ whose length belongs to $[d - \delta, d + \delta]$; (i.e., solve Problem EPL)
6. mark as safe the edges of $P$ belonging to $B$;
7. mark as safe the vertices of $P$ corresponding to trivial strongly connected components and belonging to $C$;
8. return $P$.

which there is at least one $s$-$t$ path of length $d'$. This value $d'$ is the one used in later steps. If no such value exists within a user specified distance $\delta$ to the gap length estimate (default $\delta = 500$), then the gap is left unfilled. Gap2Seq v1.0 traces back in this dynamic programming table an arbitrary $s$-$t$ path of length $d'$ (see [25], [26] for further implementation details and optimizations).

Gap2Seq v2.1 uses the values $a(v, \ell)$ computed previously, for all $\ell \leq d + \delta$, to construct the graph $G_{d,\delta}(s,t)$ and continue as in Algorithm 1. The default value for $\delta$ is, as above, $\delta = 500$. It then outputs the spelling of an arbitrary $s$-$t$ path $P$ of length $d'$, where $d'$ is chosen as above for Gap2Seq v1.0. However, in the spelling of $P$ safe bases are now marked in upper-case, and un-safe ones in lower-case. A base is considered safe if at least one $k$-mer (i.e. vertex in the de Bruijn graph) containing that base has been classified as safe. Otherwise a base is considered un-safe.

Gap2Seq v2.1 runs in parallel on the gap level, whereas Gap2Seq v1.0 is parallelized only on the scaffold level. We included a parameter (-all-upper) in Gap2Seq v2.1 which omits running Algorithm 1 and reports all filled bases in upper case, thus mimicking the behavior of Gap2Seq v1.0. In the experimental results Gap2Seq Safe denotes Gap2Seq v2.1 with default parameters and Gap2Seq denotes Gap2Seq v2.1 run with the -all-upper parameter.

We compared the quality of our method to other tools for filling gaps in scaffolds, namely GapFiller [1], SOAPdenovo’s [14] stand alone tool GapCloser, and Sealer [21] (part of the ABySS distribution). GapFiller v1.10 and GapCloser v1.12 were run with default parameters. GapFiller accepts either BOWTIE or BWA read alignments to the contigs, and we tested both versions. Sealer v1.9 was run as suggested in the manual (using parameters -k90 -k80 -k70 -k60 -k50 -k40 -k30 -j 8 -p 10). Thus, Sealer builds different de Bruijn graphs for $k \in \{90, 80, \ldots, 30\}$, and for each instance it runs the gap filler Konnector [36]. It then merges all gap filling solutions into a single solution. Parameter $P = 10$, suggested by the manual, forces Konnector to fill a gap only if there are at most 10 $s$-$t$ paths. We also tested other larger values of $P$, but $P = 10$ gave the best results: see Section 4.4.

For GapFiller and GapCloser, all bases in filled gaps were considered safe because the tools do not differentiate between safe and unsafe bases. Sealer outputs ambiguous bases using IUPAC codes and so we considered bases output as $A$, $C$, $G$ or $T$ as safe, and all other bases as unsafe. For Gap2Seq Safe we consider only bases that were declared safe by Algorithm 1. We also implemented a version of Gap2Seq in which we fill a gap only if there is a unique $s$-$t$ path of length $d$ [40], and declare all its bases as safe, which we call Gap2Seq Unique.

### 4 Experimental evaluation

We experimented with the data sets from the GAGE benchmark [27], using the scaffolds produced by nine genome assemblers for *Staphylococcus aureus*, *Rhodobacter sphaeroides* and human chromosome 14 data (hereafter called staph, rhod, and human14, respectively). The GAGE read sets from these organisms are described in Table 1. See the GAGE study [27] for details on the nine assemblers and their scaffolds. We report aggregate results over scaffolds produced by different assemblers. The detailed results for scaffolds produced by each assembler are available in the Supplementary Material. All experiments were run on a 32 GB RAM machine with 8 cores.

As observed in [26], the quality of the gap filling results heavily depends on the quality of the previous contig assembly and scaffolding steps. Thus, as done in [26], we will divide the results on human14 depending on the quality of the initial assembly. We classified these initial assemblies as: conservative, if they have less than 10 misassemblies (ABySS and SGA), moderate, if they have less than 100 misassemblies (ABySS2, Allpaths-LG, CABOG), and aggressive otherwise (Bambus2, MSR-CA, SOAPdenovo, Velvet). From the Supplementary Material one can also observe that all aggressive assemblies had in fact more than 1000 misassemblies, and also most bacterial assemblies fall into the conservative category.

### Table 1

<table>
<thead>
<tr>
<th>Organism</th>
<th>Library</th>
<th>Mean insert size</th>
<th>SD of insert size</th>
<th>Read length</th>
<th>Coverage</th>
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<tr>
<td>staph</td>
<td>short frag</td>
<td>180</td>
<td>30</td>
<td>101</td>
<td>45x</td>
</tr>
<tr>
<td>staph</td>
<td>long frag</td>
<td>3500</td>
<td>300</td>
<td>37</td>
<td>45x</td>
</tr>
<tr>
<td>rhodo</td>
<td>short frag</td>
<td>180</td>
<td>100</td>
<td>101</td>
<td>45x</td>
</tr>
<tr>
<td>rhodo</td>
<td>long frag</td>
<td>3500</td>
<td>300</td>
<td>101</td>
<td>45x</td>
</tr>
<tr>
<td>human14</td>
<td>short frag</td>
<td>135</td>
<td>20</td>
<td>101</td>
<td>42x</td>
</tr>
<tr>
<td>human14</td>
<td>long frag</td>
<td>2500</td>
<td>381</td>
<td>101</td>
<td>26x</td>
</tr>
</tbody>
</table>
4.1 Evaluating the practical strategy from Sec. 2.2

Reducing \( G_{d,\delta}(s,t) \) to its DAG of strongly connected components \( G_{d,\delta}^{SCC}(s,t) \) makes unretrievable the safe paths inside non-trivial strongly connected components. However, as shown in Table 2, most of the graphs \( G_{d,\delta}(s,t) \) do not contain any non-trivial strongly connected components (i.e., they are DAGs themselves and \( G_{d,\delta}^{SCC}(s,t) = G_{d,\delta}(s,t) \)).

Next, we tested how much overhead Algorithm 1 adds to the running time of Gap2Seq, by measuring the wall clock running time and the peak memory usage of both Gap2Seq and Gap2Seq Safe on the bacterial genomes (Table 3). We observe that the runtime increases by less than 25%. The increase in runtime is largely due to Gap2Seq Safe searching for all paths in the interval \([d - \delta, d + \delta]\), whereas Gap2Seq does not need to look for paths that deviate from \(d\) more than the optimal solution.

4.2 Evaluating the filled sequence

4.2.1 Global evaluation

There are two perspectives of evaluating the filled scaffolds. The first one is to evaluate the quality of the entire filled scaffold. This can be done by aligning it to the reference genome and measuring overall assembly metrics with a tool like QUAST [10]; e.g., NGA50 [27] and the number of misassemblies. In this case, it is undesirable to mask the unsafe bases with N's, since the safe bases may form too short sequences to be aligned reliably. This could lead to, e.g., artificially decreasing the NGA50 value or increasing the number of misassemblies. Recall also that gaps usually arise in complex, often repeated regions of the genome, making their alignment even more difficult. Thus, the safe bases outputted by Gap2Seq Safe cannot be used alone (i.e., without the unsafe ones) for a global assembly evaluation.

Considering both safe and unsafe bases is equivalent to the output of Gap2Seq v1.0.

In [25], [26] we performed a global assembly evaluation using QUAST v2.3 [10] for GapCloser, GapFiller and Gap2Seq v1.0. In the Supplementary Material of this paper we complement that evaluation with Sealer’s results. Recall that Sealer outputs ambiguous bases using IUPAC codes. For the same reason that we cannot use only safe bases in an overall evaluation, we replaced each such IUPAC code with one of the bases it encodes, at random. Sealer offers no other conversion indication, and this is also inline with e.g., Gap2Seq, which chooses a filling \(s\)-\(t\) path at random.

Tables 2 and 3 from the Supplementary Material show that Gap2Seq v1.0 generally outperforms also Sealer on the bacterial data sets. Tables 4, 5, and 6 from the Supplementary Material show that on the human14 data set Gap2Seq v1.0 outperforms Sealer on the conservative assemblies, whereas Sealer is better on the aggressive assemblies. See [26] for a detailed discussion on such an evaluation. These tables also contain the absolute numbers on the length of all gaps in the original assemblies, and the length of the filled sequences.

4.2.2 Gap-level evaluation

The second perspective is to evaluate how correct are the bases reported as safe. This pertains especially to Gap2Seq Safe, Gap2Seq Unique and Sealer. As mentioned above, we cannot align to the reference safe sequences alone, because they may be too short to be aligned reliably. Therefore, using again QUAST v2.3 [10] we produced alignments to the reference of the entire filled scaffolds. These scaffolds were the ones with both safe and unsafe bases for Gap2Seq Safe, and with IUPAC codes converted to bases for Sealer, as explained above. For Gap2Seq Unique, all bases are safe by definition. As mentioned before, for GapFiller, GapCloser and Gap2Seq v1.0 we considered all bases as being safe. For each tool, we classified each filled gap as:

- **aligned:** if QUAST reported an alignment of the gap filling sequence together with its flanking 100 bases on both sides from the filled scaffold; if a gap is closer than 100 bases from the extremity of the scaffold, the flank is that sequence until the extremity;
- **unaligned:** otherwise.

This alignment condition ensures that the filling sequence truly belongs between the corresponding flanking contigs. For example, we want to classify as an error a safe sequence in the middle of a gap that has no occurrence in the reference between its two flanking contigs. Recall again that gaps often correspond to repeated regions.

In Table 4 we show how many filled gap bases belong to unaligned filling sequences. When unable to fill a gap completely, GapCloser and GapFiller attempt to find a partial filling sequence by extending the flanking sequences. QUAST is unable to form continuous alignments for such partially filled gaps and thus, GapCloser and GapFiller produce larger amounts of filled bases that are not aligned according to the above criteria. When compared to methods producing only complete filling sequences (Sealer and Gap2Seq Unique), Gap2Seq Safe is the method penalized the most by this additional correctness condition. Nonetheless, we will see below that its performance over all gaps (aligned, unaligned or unfilled) is still better than Sealer’s and Gap2Seq Unique’s on the bacterial data sets and on conservative human assemblies.

Having an **aligned** filled sequence, we counted how many of its safe bases match the corresponding bases in the reference genome. Each such match was considered a **correct** safe base. An **incorrect** safe base is thus one that either does not belong to an aligned filling sequence, or it does not match the base to which it was aligned. Having these numbers, we computed the following accuracy metrics:

- **precision** = \[#correct safe bases / #safe bases\], where “#safe bases” is the total number of bases declared safe (in both aligned or unaligned filled gaps); thus precision measures how many of all safe bases appear in an **aligned** filling sequence and match the corresponding characters in the reference;
- **recall** = \[#correct safe bases / #total gap bases\], where “#total gap bases” is the total number of gap bases (i.e., characters N) in the original input scaffolds, independently of whether they were aligned, unaligned or unfilled; thus recall measures how many of all original gap bases appear as safe in an **aligned** filling sequence, and also match the corresponding characters in the reference.

Intuitively, precision measures how correct the safe bases are, and recall measures how much of all the gaps of the
original scaffolds was filled correctly by safe bases. Ultimately, recall is the most important metric, but at the same time bases should be declared safe with a high precision. See Table 5 and Figure 4 for results on precision and recall.

### 4.3 Evaluating complex gaps

We also evaluated how many gaps have more than 10 s-t paths of length $\ell \in [d - \delta, d + \delta]$, their proportion of all the gaps, and what is the precision and recall of Gap2Seq Safe and Sealer on these gaps. We chose the value 10 because this is the value of the parameter $P$ for which Sealer gave best results. See Table 6.

### 4.4 Evaluating Sealer for multiple bounds on the number of filling paths

We studied how Sealer’s performance is influenced by the parameter $P$, the maximum number of s-t paths allowed for a gap to be filled. Sealer’s manual suggests setting $P = 10$, but we tested $P \in \{10, 100, 1000, 10000\}$. As we can see from Table 7, the results do not improve for larger $P$. This behavior might be due to the heuristic strategy of computing an iterative alignment of the increasing number of possible filling sequences of a gap. Sealer’s running time for varying $P$ might also be explained by the additional internal choice that Sealer makes concerning the de Bruijn graph with which it works (recall that it tries $k \in \{90, 80, \ldots , 30\}$).

Since $P = 10$ gives the best results, all other experimental results concerning Sealer refer only to parameter $P = 10$.

### 5 DISCUSSION

#### 5.1 Bacterial data sets

Among the gap fillers that do not differentiate between safe and unsafe bases (GapCloser, GapFiller and Gap2Seq), Gap2Seq has the best overall precision and recall, with almost double precision and almost 8 times better recall on the rhodo data set. This is consistent with our previous results [25], [26] and due to the fact that we look for paths in the entire de Bruijn graph between the gap flanks, and that we are guided by the gap length estimate. However, we note that the precision and recall of GapCloser and GapFiller are adversely affected by the high proportion of unaligned bases, as noted in Sec. 4.2.2. Nevertheless, as discussed in Sec. 4.2.1 and Supplementary Material, Gap2Seq globally outperforms GapCloser and GapFiller.

Gap2Seq Unique provides a baseline for the performance of gap fillers distinguishing between safe and unsafe bases as even a simple method should be able to classify as safe gaps with a unique path. The precision of Gap2Seq Unique is very high but its recall, especially on rhodo, is low.

On the staph data Gap2Seq Safe has a higher precision than Sealer, but on the rhodo assemblies the precision of Sealer is higher. However, the overall recall of Gap2Seq Safe is clearly better than the recall of Sealer: 73% better recall.

---

**Table 2**

| Organism | Gaps | Gap Length | $|V_{d, \delta}(s, t)|$ | $|E_{d, \delta}(s, t)|$ | Nontrivial SCCs in $G_{d, \delta}(s, t)$ | Vertices in nontrivial SCCs in $G_{d, \delta}(s, t)$ | $|V_{d, \delta}^{SCC}(s, t)|$ | $|E_{d, \delta}^{SCC}(s, t)|$ |
|----------|------|------------|----------------|----------------|--------------------------------|--------------------------------|----------------|----------------|
| staph    | 833  | 423.0      | 1030.8         | 1043.2        | 0.197            | 417.5                       | 613.5           | 617.2          |
| rhodo    | 776  | 459.0      | 1184.0         | 1268.0        | 0.084            | 318.4                       | 865.6           | 871.3          |
| human14  | 33568 | 234.0    | 11276.1        | 11570.8       | 0.230            | 8404.5                      | 2871.9          | 2947.3         |

**Table 3**

<table>
<thead>
<tr>
<th>Gap filler</th>
<th>staph</th>
<th>rhodo</th>
<th>human14</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Runtime (s)</td>
<td>Peak memory (GB)</td>
<td>Runtime (s)</td>
</tr>
<tr>
<td>GapCloser</td>
<td>220</td>
<td>0.747</td>
<td>272</td>
</tr>
<tr>
<td>GapFiller Bowtie</td>
<td>2308</td>
<td>0.175</td>
<td>4277</td>
</tr>
<tr>
<td>GapFiller BWA</td>
<td>4034</td>
<td>0.195</td>
<td>10371</td>
</tr>
<tr>
<td>Gap2Seq</td>
<td>454</td>
<td>0.531</td>
<td>35732</td>
</tr>
<tr>
<td>Gap2Seq Safe</td>
<td>567</td>
<td>0.528</td>
<td>41652</td>
</tr>
<tr>
<td>Sealer</td>
<td>1167</td>
<td>0.528</td>
<td>1524</td>
</tr>
</tbody>
</table>

**Table 4**

<table>
<thead>
<tr>
<th>Gap filler</th>
<th>staph</th>
<th>rhodo</th>
<th>human14 (conservative)</th>
<th>human14 (moderate)</th>
<th>human14 (aggressive)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>% of total filled</td>
<td>% of total gap</td>
<td>% of total filled</td>
<td>% of total gap</td>
<td>% of total filled</td>
</tr>
<tr>
<td>GapCloser</td>
<td>10%</td>
<td>8%</td>
<td>30%</td>
<td>2%</td>
<td>28%</td>
</tr>
<tr>
<td>GapFiller Bowtie</td>
<td>63%</td>
<td>9%</td>
<td>69%</td>
<td>2%</td>
<td>53%</td>
</tr>
<tr>
<td>GapFiller BWA</td>
<td>57%</td>
<td>10%</td>
<td>64%</td>
<td>4%</td>
<td>52%</td>
</tr>
<tr>
<td>Gap2Seq</td>
<td>14%</td>
<td>12%</td>
<td>7%</td>
<td>2%</td>
<td>5%</td>
</tr>
<tr>
<td>Sealer</td>
<td>11%</td>
<td>4%</td>
<td>1%</td>
<td>0%</td>
<td>1%</td>
</tr>
<tr>
<td>Gap2Seq Safe</td>
<td>15%</td>
<td>12%</td>
<td>8%</td>
<td>2%</td>
<td>5%</td>
</tr>
<tr>
<td>Gap2Seq Unique</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
</tr>
</tbody>
</table>
TABLE 5
Precision and recall. We show aggregate values over all assemblies. Sealer was run for a week on the SGA assembly of staph and it did not finish. The gaps in the SGA assembly of staph on which Sealer did not finish running were not used to penalize its recall. We marked in bold the best results among rows 1–4, and among rows 5–8, respectively.

<table>
<thead>
<tr>
<th>Gap filler</th>
<th>staph precision recall</th>
<th>rhodo precision recall</th>
<th>human14 (conservative) precision recall</th>
<th>human14 (moderate) precision recall</th>
<th>human14 (aggressive) precision recall</th>
</tr>
</thead>
<tbody>
<tr>
<td>GapCloser</td>
<td>0.839 0.449</td>
<td>0.587 0.027</td>
<td>0.714 0.079</td>
<td>0.379 0.060</td>
<td>0.242 0.079</td>
</tr>
<tr>
<td>GapFiller Bowtie</td>
<td>0.365 0.049</td>
<td>0.296 0.008</td>
<td>0.459 0.232</td>
<td>0.378 0.069</td>
<td>0.186 0.045</td>
</tr>
<tr>
<td>GapFiller BWA</td>
<td>0.424 0.078</td>
<td>0.341 0.020</td>
<td>0.478 0.269</td>
<td>0.339 0.078</td>
<td>0.171 0.056</td>
</tr>
<tr>
<td>Gap2Seq</td>
<td>0.841 0.668</td>
<td>0.918 0.265</td>
<td>0.947 0.243</td>
<td>0.732 0.138</td>
<td>0.663 0.026</td>
</tr>
<tr>
<td>Sealer</td>
<td>0.891 0.291</td>
<td>0.979 0.034</td>
<td>0.986 0.120</td>
<td>0.922 0.057</td>
<td>0.869 0.039</td>
</tr>
<tr>
<td>Gap2Seq Safe</td>
<td>0.952 0.503</td>
<td>0.949 0.172</td>
<td>0.968 0.216</td>
<td>0.795 0.089</td>
<td>0.763 0.022</td>
</tr>
<tr>
<td>Gap2Seq Unique</td>
<td>1.000 0.250</td>
<td>0.996 0.063</td>
<td>0.995 0.090</td>
<td>0.989 0.006</td>
<td>0.811 0.012</td>
</tr>
</tbody>
</table>

Fig. 4. Precision and recall of the gap fillers for each assembly of staph, rhodo, and human14. See the supplementary material for the exact values for each assembly.

TABLE 6
Precision and recall of Gap2Seq Safe and Sealer, when restricted to gaps where Gap2Seq finds more than 10 s-t paths of length $\ell \in [d - \delta, d + \delta]$. The percentages in columns 2 and 3 indicate the ratio of the total number of gaps, and of the total gap length of the assembly, respectively. Recall is relative to these gaps with more than 10 paths.

<table>
<thead>
<tr>
<th>Data set</th>
<th>No. of gaps</th>
<th>Sum of gap lengths</th>
<th>Gap2Seq Safe Precision</th>
<th>Gap2Seq Safe Recall</th>
<th>Sealer Precision</th>
<th>Sealer Recall</th>
</tr>
</thead>
<tbody>
<tr>
<td>staph</td>
<td>2632 (25%)</td>
<td>15828 (26%)</td>
<td>0.858 0.365</td>
<td>0.087</td>
<td>0.227</td>
<td></td>
</tr>
<tr>
<td>rhodo</td>
<td>143 (5%)</td>
<td>122529 (8%)</td>
<td>0.802 0.443</td>
<td>0.958</td>
<td>0.077</td>
<td></td>
</tr>
<tr>
<td>human14 conservative</td>
<td>2370 (11%)</td>
<td>911254 (7%)</td>
<td>0.879 0.693</td>
<td>0.968</td>
<td>0.238</td>
<td></td>
</tr>
<tr>
<td>human14 moderate</td>
<td>1175 (12%)</td>
<td>647165 (15%)</td>
<td>0.751 0.427</td>
<td>0.852</td>
<td>0.113</td>
<td></td>
</tr>
<tr>
<td>human14 aggressive</td>
<td>4265 (5%)</td>
<td>1063668 (1%)</td>
<td>0.615 0.391</td>
<td>0.913</td>
<td>0.265</td>
<td></td>
</tr>
</tbody>
</table>

TABLE 7
Precision, recall and total running time of Sealer, over all assemblies on staph and rhodo, for varying values of its $P$ parameter.

<table>
<thead>
<tr>
<th>$P$</th>
<th>staph</th>
<th>rhodo</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>staph</td>
<td>rhodo</td>
<td>Precision</td>
<td>Recall</td>
</tr>
<tr>
<td>10</td>
<td>0.891</td>
<td>0.291</td>
<td>1167</td>
<td>0.034</td>
</tr>
<tr>
<td>100</td>
<td>0.863</td>
<td>0.278</td>
<td>893</td>
<td>0.034</td>
</tr>
<tr>
<td>1000</td>
<td>0.683</td>
<td>0.278</td>
<td>931</td>
<td>0.033</td>
</tr>
<tr>
<td>10000</td>
<td>0.681</td>
<td>0.278</td>
<td>918</td>
<td>0.033</td>
</tr>
</tbody>
</table>
on staph, and 406% better recall on rhodo. Our experiments suggest this is the case because Gap2Seq Safe scales to gaps where the number of paths is large. Indeed, Table 6 (and recall also Fig. 1) shows that a non-negligible proportion of the total gap length is complex, and Gap2Seq Safe has a precision and recall consistent with the full results. Table 6 shows that Sealer is able to deal with some of these complex gaps because it tries filling them for multiple values of $k$. However, especially on the rhodo data set, the recall of Sealer is low. Note that the same heuristic strategy of using multiple values of $k$ could also be applied to Gap2Seq, but then it is harder to define what a safe base is.

Comparing the best of the above two categories (i.e., Gap2Seq and Gap2Seq Safe), we observe that Gap2Seq Safe is able to correctly classify as safe a large proportion of the total gap length correctly retrievable by Gap2Seq. This shows that our definition of safe filling path is a well-motivated one. Recall also that the output of Gap2Seq Safe also contains the unsafe bases. Thus the remaining sequences that add up to the recall of Gap2Seq come from bubbles and other more complex regions of the assembly graph. We leave it as future work to identify and extract the safe bases from these regions. The precision of Gap2Seq Safe is better than that of Gap2Seq on most assemblies, with a more significant increase on staph than on rhodo.

5.2 Human14 data set

As observed also in [26], the results on human assemblies heavily depend on the quality of the initial assembly. For example, on the ABysS assembly (conservative), Gap2Seq generally fills paths or reports that no path exists, whereas on the SOAPPdenovo assembly (aggressive), Gap2Seq abandons many longer gaps because it exceeds the memory limit [26, Fig. 5].

On the conservative and moderate assemblies, where Gap2Seq outperforms Sealer in the global evaluation (recall Sec. 4.2.1), we see that also Gap2Seq Safe generally outperforms Sealer on the gap level evaluation (Table 5): on conservative assemblies Gap2Seq Safe has almost double recall, with a small drop in precision, and on moderate assemblies Gap2Seq maintains the double recall, with a larger drop in precision. This suggests that Sealer avoids making wrong predictions by not filling complex gaps with many paths. This interpretation is also supported by the drop in recall. Similar to the results on bacterial genomes, Table 6 shows that Gap2Seq Safe can fill many complex gaps with safe bases correctly. Sealer is also able to fill some of these gaps due to its strategy of trying multiple values of $k$ but it clearly has a lower recall than Gap2Seq Safe.

We also observe that Gap2Seq Safe has a similar behavior with respect to Gap2Seq as in bacterial genomes. Namely, the precision always increases, with only a slight drop in recall.

To conclude, Gap2Seq Safe is naturally limited by the performance of Gap2Seq, which is best seen on complex gaps and on aggressive assemblies. On correct initial human14 assemblies, Gap2Seq Safe shows a similar behavior as in the bacterial data sets.

6 Conclusion

In this paper we studied safe (partial) solutions to a gap filling instance, and showed that they are well-motivated in practice, especially on correct initial assemblies. Indeed, on bacterial genomes and on conservative human assemblies, our method can detect as reliable at least 73% more gap bases as compared to the few previous methods distinguishing between ambiguous and unambiguous filling bases, with a comparable precision level.

To improve the runtime of Gap2Seq, we could apply a similar approach as when extending Gap2Seq for genotyping insertions [39]. Similar to GapFiller [1], for each gap we would first determine a subset $R'$ of reads whose mates align on the flanks of the gap. The traversal of the graph when closing this particular gap would then be limited to those vertices derived from the reads $R'$.

Our method outputs entire filling sequences—thus being compatible with later downstream analyses—but it cannot improve global assembly metrics such as NGA50. However, by marking the safe bases, it can provide a more informed answer on the gap filling sequence. This is a challenging problem considering that gaps arise in complex regions of a genome.


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