Supplementary Material for
User-Level Implementations of Read-Copy Update

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APPENDIX

A. User-Space RCU Desiderata

Extensive use of RCU within the practitioner community has led to the following user-space RCU desiderata:

1) RCU read-side primitives must have $O(1)$ computational complexity with a small constant, thus enabling real-time use and avoiding lock-based deadlocks. “Small constant” means avoiding expensive operations such as cache misses, atomic instructions, memory barriers, and, where feasible, conditional branches [1].

2) RCU read-side primitives should be usable in all contexts, including nested within other RCU read-side critical sections and inside user-level signal handlers [2].

3) RCU read-side primitives must be unconditional, with neither failure nor retry, thus avoiding livelocks [3].

4) RCU readers must not starve writers, even given arbitrarily high rates of time-bounded read-side critical sections.

5) RCU read-side critical sections may not contain operations that wait for a grace period, such as synchronize_rcu() (it would self-deadlock), nor may they acquire locks that are held across calls to synchronize_rcu(). However, non-interfering lock acquisition/release and other non-idempotent operations such as I/O should be permitted [4].

6) Mutating RCU-protected data structures must be permitted within RCU read-side critical sections, for example by acquiring the lock used to protect updates [4]. Such lock acquisitions can be thought of as unconditional read-to-write upgrades. However, any lock acquired within a read-side critical section cannot be held while waiting for a grace period.

7) RCU primitives should be independent of memory allocator design and implementation [3].

Although in-kernel RCU implementations are common, making them available to user applications is not practical. Firstly, many kernel-level RCU implementations assume that RCU read-side critical sections cannot be preempted, which is not the case at user level. Secondly, a user application invoking kernel-level RCU primitives could hang the system by remaining in an RCU read-side critical section indefinitely. Finally, invoking any in-kernel RCU implementation from user-level code introduces system-call overhead, violating the first desideratum above.

In contrast, the RCU implementations described in Appendix D are designed to meet the above list of desiderata with acceptably low overheads.

B. Example RCU Use Case

Consider a real-time closed-loop control application governed by a complex mathematical control law, where the control loop must execute at least every 100 microseconds. Suppose that this control law is too computationally expensive to be computed each time through the control loop, so a simpler linear approximation is used instead. As environmental parameters (such as temperature) slowly change, a new linear approximation must be computed from the full mathematical control law. Therefore, a lower-priority task computes a set of three coefficients for the linear approximation periodically, for example, every five seconds. The control-loop task then makes use of the most recently produced set of coefficients.

Of course, it is critically important that each control-loop computation use a consistent set of coefficients. It is therefore necessary to use proper synchronization between the control...
loop and the production of a new set of coefficients. In contrast, use of a slightly outdated set of coefficients is acceptable. We can therefore use RCU to carry out the synchronization, as shown in the (fanciful) implementation in Figure 1. The overall approach is to periodically publish a new set of coefficients to synchronize_rcu(). The synchronized rcu() primitive is used to prevent overwriting a set of coefficients that is still in use. Because only one thread will be updating the coefficients, update-side synchronization is not required.

The control_loop() function is invoked from the thread performing closed-loop control. It first invokes rcu_register_thread() to make itself known to RCU, and then enters an infinite loop performing the real-time control actions. Each pass through this loop first measures the control input value, then enters an RCU read-side critical section to obtain the current set of coefficients, uses lin_approx() to compute a new control value, uses do_control() to output this value, and finally does a 50-microsecond delay. The use of rcu_dereference() ensures that the coefficients will be fully initialized, even on weakly ordered systems, and the use of rcu_read_lock() and rcu_read_unlock() ensure that subsequent grace periods cannot complete until the coefficients are completely copied.

The lin_approx_loop() function is invoked from the thread that is to periodically compute a new set of coefficients for use by control_loop(). As with control_loop(), it first invokes rcu_register_thread() to make itself known to RCU, and then enters an infinite loop performing the coefficient calculations. To accomplish this, it defines an array of two sets of coefficients along with an index that selects which of the two sets is currently in effect. Each pass through the loop computes a new set of coefficients into the element of the array that is not currently being used by readers, uses rcu_assign_pointer() to publish this new set, uses synchronize_rcu() to wait for control_loop() to finish using the old set, and finally waits for five seconds before repeating this process.

Because rcu_dereference() is wait-free with small overhead, this approach is well-suited to real-time systems running on multi-core systems. In contrast, approaches based on locking would require control_loop() to wait on lin_approx_loop() when the latter was installing a new set of coefficients, meaning that they might be subject to priority inversion.

### C. Overview of RCU Semantics

RCU semantics comprise the grace-period guarantee and the publication guarantee. As noted earlier, concurrent modifications of an RCU-protected data structure must be coordinated by some other mechanism, for example, locking.

#### 1) Grace-Period Guarantee:

As noted in the printed paper, RCU read-side critical sections are delimited by rcu_read_lock() and rcu_read_unlock(), and RCU grace periods are periods of time such that all RCU read-side critical sections in existence at the beginning of a given grace period have completed before its end.

Somewhat more formally, consider a group of statements \( R_i \) within a single RCU read-side critical section:

\[
\text{rcu_read_lock}(); \quad R_0; R_1; R_2; \ldots; \quad \text{rcu_read_unlock}();
\]

Consider also groups of statements \( M_m \) (some of which may mutate shared data structures) and \( D_n \) (some of which may destroy shared data structures) separated by synchronize_rcu():

\[
M_0; M_1; M_2; \ldots; \text{synchronize_rcu}(); D_0; D_1; D_2; \ldots;
\]

Then the following holds, where "\( \rightarrow \)" indicates that the statement on the left executes prior to that on the right:

\[
\forall m, i(M_m \rightarrow R_i) \lor \forall i, n(R_i \rightarrow D_n).
\]

In other words, a given read-side critical section cannot extend beyond both sides of a grace period. Formulas 2 and 3 follow straightforwardly and are often used to validate uses of RCU ("\( \Rightarrow \)" denotes logical implication):

\[
\exists i, m(R_i \rightarrow M_m) \Rightarrow \forall j, n(R_j \rightarrow D_n),
\]

\[
\exists n, i(D_n \rightarrow R_i) \Rightarrow \forall m, j(M_m \rightarrow R_j).
\]

In other words, if any statement in a given read-side critical section executes prior to any statement preceding a given grace period, then all statements in that critical section must execute prior to any statement following this same grace period. Conversely, if any statement in a given read-side critical section executes after any statement following a given grace period, then all statements in that critical section must execute after any statement preceding this same grace period. A striking pictorial representation of this grace-period guarantee is shown in Figure 2 of the printed paper.

This guarantee permits RCU-based algorithms to trivially avoid a number of difficult race conditions whose resolution can otherwise result in poor performance, limited scalability, and great complexity. However, on weakly ordered systems this guarantee is insufficient. We also need some way to guarantee that if a reader sees a pointer to a new data structure, it will also see the values stored during initialization of that structure. This guarantee is presented in the next section.

2This description is deliberately vague. More-precise definitions of "\( A \rightarrow B \)" [5, Section 1.10] consider the individual memory locations accessed by both \( A \) and \( B \), and order the two statements with respect to each of those accesses. For our purposes, what matters is that \( A \rightarrow B \) and \( B \rightarrow A \) can’t both hold. If \( A \) and \( B \) execute concurrently then both relations may fail. However as a special case, if \( A \) is a store to a variable and \( B \) is a load from that same variable, then either \( A \rightarrow B \) (\( B \) reads the value stored by \( A \) or a later value) or \( B \rightarrow A \) (\( B \) reads a value prior to that stored by \( A \)).

3Some RCU implementations may choose to weaken this guarantee so as to exclude special-purpose operations such as MMIO accesses, I/O-port instructions, and self-modifying code. Such weakening is appropriate on systems where ordering these operations is expensive and where the users of that RCU implementation either (1) are not using these operations or (2) insert the appropriate ordering into their own code, as many system calls do.
2) Publication Guarantee: Note well that the statements $R_i$ and $M_m$ may execute concurrently, even in the case where $R_i$ is referencing the same data element that $M_m$ is concurrently modifying. The publication guarantee provided by \texttt{rcu_assign_pointer()} and \texttt{rcu_dereference()} handles this concurrency correctly and easily: even on weakly ordered systems, any dereference of a pointer returned by \texttt{rcu_dereference()} is guaranteed to see any change prior to the corresponding \texttt{rcu_assign_pointer()}, including any change prior to any earlier \texttt{rcu_assign_pointer()} involving that same pointer.

Somewhat more formally, suppose that \texttt{rcu_assign_pointer()} is used as follows:

\[ I_0; I_1; I_2; \ldots; \texttt{rcu_assign_pointer}(g,p); \]

where each $I_i$ is a statement (including those initializing fields in the structure referenced by local pointer $p$), and where global pointer $g$ is visible to reading threads. This initialization sequence is part of the $M_m$ sequence of statements discussed earlier.

The body of a canonical RCU read-side critical section would appear as follows:

\[ \ldots; q = \texttt{rcu_dereference}(g); A_0; A_1; A_2; \ldots; \]

where $q$ is a local pointer, $g$ is the same global pointer updated by the earlier \texttt{rcu_assign_pointer()} (and possibly updated again by later invocations of \texttt{rcu_assign_pointer()}), and some of the $A_i$ statements dereference $q$ to access fields initialized by some of the $I_i$ statements. This sequence of \texttt{rcu_dereference()} followed by $A_i$ statements is part of the $R_i$ statements discussed earlier.

Then we have the following, where $M$ is the \texttt{rcu_assign_pointer()} and $R$ is the \texttt{rcu_dereference()}:

\[ M \rightarrow R \implies \forall i, j(I_i \rightarrow A_j). \tag{4} \]

In other words, if a given \texttt{rcu_dereference()} statement accesses the value stored to $g$ by a given \texttt{rcu_assign_pointer()}, then all statements dereferencing the pointer returned by that \texttt{rcu_dereference()} must see the effects of any initialization statements preceding that \texttt{rcu_assign_pointer()} or any earlier \texttt{rcu_assign_pointer()} storing to $g$.

This guarantee provides readers a consistent view of newly added data.

3) Uses of RCU Guarantees: These grace-period and publication guarantees are extremely useful, but in ways that are not always immediately obvious. This section therefore describes a few of the most common uses of these guarantees.

First, they can provide existence guarantees [6], so that any RCU-provided data element accessed anywhere within a given RCU read-side critical section is guaranteed to remain intact throughout that RCU read-side critical section. Existence guarantees are provided by ensuring that an RCU grace period elapses between the moment a given data element is rendered inaccessible to readers and the moment this element’s memory is reclaimed and/or reused.

Second, the RCU guarantees can provide type-safe memory [7] by integrating RCU grace periods into the memory allocator—for example, the Linux kernel’s slab allocator provides type-safe memory when the SLAB_DESTROY_BY_RCU flag is specified. This integration is accomplished by permitting a freed data element to be immediately reused, but only if its type remains unchanged. The allocator must ensure that an RCU grace period elapses before that element’s type is permitted to change. This approach guarantees that any data element accessed within a given RCU read-side critical section retains its type throughout that RCU read-side critical section.

Finally, as noted earlier, RCU’s grace-period and publication guarantees can often be used to replace reader-writer locking.

As a result, the grace-period and publication guarantees enable a wide variety of algorithms and data structures providing extremely low read-side overheads for read-mostly data structures [8, 2, 9, 1]. Again, note that concurrent updates must be handled by some other synchronization mechanism.

With this background on RCU, we are ready to consider how it might be used in user-level applications.

D. Classes of RCU Implementations

This section describes several classes of RCU implementations. Appendix D1 first describes some primitives that might be unfamiliar to the reader, and then Appendix D2, D3, and D4 present user-space RCU implementations that are optimized for different use cases. The QSBR implementation presented in Appendix D2 offers the best possible read-side performance, but requires that each thread periodically calls a function to announce that it is in a quiescent state, thus strongly constraining the application’s design. The implementation presented in Appendix D3 places almost no constraints on the application’s design, thus being appropriate for use within a general-purpose library, but it has higher read-side overhead. Appendix D4 presents an implementation having low read-side overhead and requiring only that the application give up one POSIX signal to RCU update processing. Finally, Appendix D5 demonstrates how to create non-blocking RCU update primitives.

We start with a rough overview of some elements common to all three implementations. A global variable, \texttt{rcu_gp_ctr}, tracks grace periods. Each thread has a local variable indicating whether or not it is currently in a read-side critical section, together with a snapshot of \texttt{rcu_gp_ctr’s} value at the time the read-side critical section began. The \texttt{synchronize_rcu()} routine iterates over all threads, using these snapshots to wait so long as any thread is in a read-side critical section that started before the current grace period.

Grace periods can be tracked in two different ways. The simplest method, used in Appendix D2, is for \texttt{rcu_gp_ctr} simply to count grace periods. Because of the possibility of counter overflow, this method is suitable only for 64-bit architectures. The other method divides each grace period up into two phases and makes \texttt{rcu_gp_ctr} track the current phase. As explained in Appendix D3 below, this approach avoids the problem of counter overflow at the cost of prolonging grace periods; hence it can be used on all architectures.
izes grace-period detection and updates of the global grace-period counter. The 
pthread_mutex_t type is defined by the pthread library for mutual exclusion variables; the mutex_lock() primitive acquires a pthread_mutex_t instance and mutex_unlock() releases it. Line 11 introduces the rcu_reader per-thread variable, through which each access to per-thread registry information is performed. These per-thread variables are declared via the _thread storage-class specifier, as specified by C99 [10], and as extended by gcc to permit cross-thread access to per-thread variables. The tid field of struct rcu_reader entry contains the thread identifier returned by pthread_self(). This identifier is used to send signals to specific threads by signal-based RCU, presented in Appendix D4. The need_mb field is also used by the signal-based RCU implementation to keep track of threads which have executed their signal handlers. The rcu_thread_online() and rcu_thread_offline() primitives mark the online status of reader threads and are specific to the QSBR RCU implementation shown in Appendix D2.

2) Quiescent-State-Based Reclamation RCU: The QSBR RCU implementation provides near-zero read-side overhead, as has been presented earlier [8]. This section expands on that work by describing a similar QSBR implementation for 64-bit systems. The price of minimal overhead is that each thread in an application is required to periodically invoke rcu_quiescent_state() to announce that it resides in a quiescent state. This requirement can entail extensive application modifications, limiting QSBR’s applicability.

QSBR uses these quiescent-state announcements to approximate the extent of read-side critical sections, treating the interval between two successive announcements as a single, large critical section. As a consequence, the rcu_read-

1) Common Primitives: This section describes a number of primitives that are used by examples in later sections.

Figure 2 introduces primitives dealing with shared memory at the compiler level. The ACCESS_ONCE() primitive applies volatile semantics to its argument. The LOAD_SHARED() primitive prohibits any compiler optimization that might otherwise turn a single load into multiple loads (as might happen under heavy register pressure), and vice versa. The STORE_SHARED() primitive acts as an assignment statement, but prohibits any compiler optimization that might otherwise turn a single store into multiple stores and vice versa. The barrier() primitive prohibits any compiler code-motion optimization that might otherwise move loads or stores across the barrier(). Among other things, we use it to force the compiler to reload values on each pass through a wait loop. It is strictly a compiler directive; it emits no code.

The smp_mb() primitive (not shown in Figure 2 because its implementation is architecture-specific) emits a full memory barrier, for example, the sync instruction on the PowerPC architecture (“mb” stands for “memory barrier”). The fundamental ordering property of memory barriers can be expressed as follows: Suppose one thread executes the statements

\[ A_0; A_1; A_2; \ldots; \text{smp_mb}(); B_0; B_1; B_2; \ldots; \]

and another thread executes the statements

\[ C_0; C_1; C_2; \ldots; \text{smp_mb}(); D_0; D_1; D_2; \ldots; \]

Then \( \exists m, n (B_m \rightarrow C_n) \) implies \( \forall i, j (A_i \rightarrow D_j) \).

These primitives can be expressed directly in terms of the upcoming C++0X standard [5]. For the smp_mb() primitive this correspondence is not exact; our memory barriers are somewhat stronger than the standard’s atomic_thread_fence (memory_order_seq_cst). The LOAD_SHARED() primitive maps to x.load (memory_order_relaxed) and STORE_SHARED() to x.store (memory_order_relaxed). The barrier() primitive maps to atomic_signal_fence (memory_order_seq_cst). In addition, rcu_dereference() maps to x.load (memory_order_consume) and rcu_assign_pointer() maps to x.store (memory_order_release).

Figure 3 introduces declarations and data structures used by all implementations, along with the process-wide registry tracking all threads containing RCU read-side critical sections. The pthread mutex rcu_gp_lock (lines 1–2) serializes addition (line 17), removal (line 26) and iteration (which will be presented in Figures 5, 7, and 10) on the reader thread list (list head is at line 3 and nodes at line 8 of Figure 3). This rcu_gp_lock also serializes grace-period detection and updates of the global grace-period counter. The pthread_mutex_t type is defined by the pthread library for mutual exclusion variables; the mutex_lock() primitive acquires a pthread_mutex_t instance and mutex_unlock() releases it. Line 11 introduces the rcu_reader per-thread variable, through which each access to per-thread registry information is performed. These per-thread variables are declared via the _thread storage-class specifier, as specified by C99 [10], and as extended by gcc to permit cross-thread access to per-thread variables. The tid field of struct rcu_reader entry contains the thread identifier returned by pthread_self(). This identifier is used to send signals to specific threads by signal-based RCU, presented in Appendix D4. The need_mb field is also used by the signal-based RCU implementation to keep track of threads which have executed their signal handlers. The rcu_thread_online() and rcu_thread_offline() primitives mark the online status of reader threads and are specific to the QSBR RCU implementation shown in Appendix D2.

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QSBR uses these quiescent-state announcements to approximate the extent of read-side critical sections, treating the interval between two successive announcements as a single, large critical section. As a consequence, the rcu_read-
lock() and rcu_read_unlock() primitives need do nothing and will often be inlined and optimized away, as in fact they are in server builds of the Linux kernel. QSBR thus provides unsurpassed read-side performance, albeit at the cost of longer grace periods. When QSBR is being used to reclaim memory, these longer grace periods result in more memory being consumed by data structures waiting for grace periods, in turn resulting in the classic CPU-memory tradeoff.

The 64-bit global counter rcu_gp_ctr shown in Figure 4 contains 1 in its low-order bit and contains the current grace-period number in its remaining bits. It may be accessed at any time by any thread but may be updated only by the thread holding rcu_gp_lock. The rcu_quiescent_state() function simply copies a snapshot of the global counter to the per-thread rcu_reader.ctr variable (which may be modified only by the corresponding thread). The 1 in the low-order bit serves to indicate that the reader thread is not in an extended quiescent state. The two memory barriers enforce ordering of preceding and subsequent accesses.

As an alternative to periodically invoking rcu_quiescent_state(), threads may use the rcu_thread_offline() and rcu_thread_online() APIs to mark the beginnings and ends of extended quiescent states. These three functions must not be called from within read-side critical sections. The rcu_thread_offline() function simply sets the per-thread rcu_reader.ctr variable to zero, indicating that this thread is in an extended quiescent state. Memory ordering is needed only at the beginning of the function because the following code cannot be in a read-side critical section. The rcu_thread_online() function is similar to rcu_quiescent_state(), except that it requires a memory barrier only at the end. Note that all the functions in Figure 4 are wait-free because they each execute a fixed sequence of instructions.

Figure 5 shows synchronize_rcu() and its two helper functions, update_counter_and_wait() and rcu_gp_ongoing(). The synchronize_rcu() function puts the current thread into an extended quiescent state if it is not already in one, forces ordering of the caller’s accesses, and invokes update_counter_and_wait() under the protection of rcu_gp_lock. The update_counter_and_wait() function increments the global rcu_gp_ctr variable by 2 (recall that the lower bit is reserved for readers to indicate whether they are in an extended quiescent state). It then uses list_for_each_entry() to scan all of the threads, invoking rcu_gp_ongoing() on each, thus waiting until all threads have exited any pre-existing RCU read-side critical sections. The barrier() macro on line 23 prevents the compiler from checking the threads before updating rcu_gp_ctr, which could result in deadlock. The usleep() function on line 26 blocks for the specified number of milliseconds, in this case chosen arbitrarily. Finally, the rcu_gp_ongoing() function checks to see if the specified counter indicates that the corresponding thread might be in a pre-existing RCU read-side critical section. It accomplishes this with the two-part check on line 35: if the counter is zero, the thread is in an extended quiescent state, while if the counter

```c
#define RCU_GP_ONLINE 0x1
#define RCU_GP_CTR 0x2

unsigned long rcu_gp_ctr = RCU_GP_ONLINE;

static inline void rcu_read_lock(void)
{
    smp_mb();
    STORE_SHARED(rcu_reader.ctr, LOAD_SHARED(rcu_gp_ctr));
    smp_mb();
}

static inline void rcu_read_unlock(void)
{
    smp_mb();
    LOAD_SHARED(rcu_gp_ctr);
    smp_mb();
}

static inline void rcu_quiescent_state(void)
{
    smp_mb();
    STORE_SHARED(rcu_gp_ctr, rcu_gp_ctr + RCU_GP_CTR);
    barrier();
    list_for_each_entry(index, &registry, node) {
        barrier();
        while (rcu_gp_ongoing(&index->ctr))
            msleep(10);
    }
}

static inline void rcu_thread_offline(void)
{
    struct rcu_reader *index;
    if (was_online)
        update_counter_and_wait();
    if (was_online)
        STORE_SHARED(rcu_reader.ctr, rcu_gp_ctr + RCU_GP_CTR);
    barrier();
    list_for_each_entry(index, &registry, node) {
        barrier();
        while (rcu_gp_ongoing(index->ctr))
            msleep(10);
    }
}

static inline void rcu_thread_online(void)
{
    smp_mb();
    LOAD_SHARED(rcu_gp_ctr);
    smp_mb();
}

static inline void rcu_thread_offline(void)
{
    struct rcu_reader *index;
    if (was_online)
        update_counter_and_wait();
    if (was_online)
        STORE_SHARED(rcu_reader.ctr, rcu_gp_ctr + RCU_GP_CTR);
    barrier();
    list_for_each_entry(index, &registry, node) {
        barrier();
        while (rcu_gp_ongoing(index->ctr))
            msleep(10);
    }
}

static inline void rcu_quiescent_state(void)
{
    smp_mb();
    STORE_SHARED(rcu_gp_ctr, rcu_gp_ctr + RCU_GP_CTR);
    barrier();
    list_for_each_entry(index, &registry, node) {
        barrier();
        while (rcu_gp_ongoing(index->ctr))
            msleep(10);
    }
}

void synchronize_rcu(void)
{
    unsinged long was_online;
    was_online = rcu_reader.ctr;
    smp_mb();
    if (was_online)
        STORE_SHARED(rcu_reader.ctr, rcu_gp_ctr);
    mutex_lock(rcu_gp_lock);
    update_counter_and_wait();
    mutex_unlock(rcu_gp_lock);
    if (was_online)
        STORE_SHARED(rcu_reader.ctr,
        LOAD_SHARED(rcu_gp_ctr));
    smp_mb();
}
```

Fig. 4. RCU Read Side Using Quiescent States

Fig. 5. RCU Update Side Using Quiescent States
is equal to \texttt{rcu\_gp\_ctr}, the thread is in an RCU read-side critical section that began after beginning of the current RCU grace period, and therefore need not be waited for.

We specify a 64-bit \texttt{rcu\_gp\_ctr} to avoid overflow. The fundamental issue is that there is no way to copy a value from one memory location to another atomically. Suppose reader thread \texttt{T} is preempted just before executing the \texttt{STORE\_SHARED()} call in \texttt{rcu\_thread\_online()}, after the \texttt{LOAD\_SHARED()} call has returned. Until the store takes place the thread is still in its extended quiescent state, so there is nothing to prevent other threads from making multiple calls to \texttt{synchronize\_rcu()} (and thereby incrementing \texttt{rcu\_gp\_ctr}) during the preemption delay. If the counter cycles through all but one of its values, the stale value finally stored in thread \texttt{T}'s \texttt{rcu\_reader.ctr} will actually be \texttt{rcu\_gp\_ctr}'s next value. As a result, if another thread later calls \texttt{synchronize\_rcu()} after \texttt{T} has entered a read-side critical section, then \texttt{update\_counter\_and\_wait()} might return before \texttt{T} has left this critical section, in violation of RCU's semantics. With 64 bits, thousands of years would be required to overflow the counter and hence the possibility may be ignored. However, given a 32-bit \texttt{rcu\_gp\_ctr} this scenario is possible; hence 32-bit implementations should instead adapt the two-phase scheme discussed in Appendix D3 [13].

Given that they are empty functions, the \texttt{rcu\_read\_lock()} and \texttt{rcu\_read\_unlock()} primitives are wait-free under the most severe conceivable definition [14]. Because it waits for pre-existing readers, \texttt{synchronize\_rcu()} is not non-blocking. Appendix D5 describes how RCU updates can support non-blocking algorithms in the same sense as they are supported by garbage collectors.

The need for periodic \texttt{rcu\_quiescent\_state()} invocations can make QSBR impossible to use in some situations, such as within libraries. In addition, this QSBR implementation does not allow concurrent \texttt{synchronize\_rcu()} calls to share grace periods—a straightforward optimization, but beyond the scope of this paper. That said, this code can form the basis for a production-quality RCU implementation [13].

Another limitation of the quiescent-state approach is that applications requiring read-side critical sections in signal handlers must disable signals around invocation of \texttt{rcu\_quiescent\_state()}, and for the duration of extended quiescent states marked by \texttt{rcu\_thread\_offline()} and \texttt{rcu\_thread\_online()}. In addition, applications needing to invoke \texttt{synchronize\_rcu()} while holding a lock must ensure that all acquisitions of that lock invoke \texttt{rcu\_thread\_offline()}, presumably via a wrapper function encapsulating the lock-acquisition primitive. Applications needing read-side critical sections within signal handlers or that need to invoke \texttt{synchronize\_rcu()} while holding a lock might therefore be better served by the RCU implementations described in subsequent sections.

A semi-formal verification that this implementation satisfies the grace-period guarantee (in the absence of overflow) is presented in Appendix F.

The next section discusses an RCU implementation that is safe for use in libraries, the tradeoff being higher read-side overhead.

1 \#define RCU\_GP\_CTR\_PHASE 0x10000
2 \#define RCU\_NEST\_MASK 0x0fff
3 \#define RCU\_NEST\_COUNT 0x1
4
5 unsigned long rcu\_gp\_ctr = RCU\_NEST\_COUNT;
6
7 static inline void rcu\_read\_lock(void)
8 { 9 unsigned long tmp;
10
11 tmp = rcu\_reader.ctr;
12 if (!((tmp & RCU\_NEST\_MASK)) { 13 STORE\_SHARED(rcu\_reader.ctr, 14 LOAD\_SHARED(rcu\_gp\_ctr)); 15 smp\_mb(); 16 } else {
17 STORE\_SHARED(rcu\_reader.ctr, tmp + RCU\_NEST\_COUNT);
18 }
19 }
20
21 static inline void rcu\_read\_unlock(void)
22 { 23 smp\_mb(); 24 STORE\_SHARED(rcu\_reader.ctr, 25 rcu\_reader.ctr - RCU\_NEST\_COUNT);
26 }

Fig. 6. RCU Read Side Using Memory Barriers

3) General-Purpose RCU: The general-purpose RCU implementation can be used in any software environment, including library functions that are not aware of the design of the calling application. Such library functions cannot guarantee that each application’s threads will invoke \texttt{rcu\_quiescent\_state()} sufficiently often, nor can they ensure that threads will invoke \texttt{rcu\_thread\_offline()} and \texttt{rcu\_thread\_online()} around each blocking system call. General-purpose RCU therefore does not require that these three functions ever be invoked.

In addition, this general-purpose implementation avoids the counter-overflow problem discussed in Appendix D2 by using a different approach to track grace periods. Each grace period is divided into two grace-period phases, and instead of a free-running grace-period counter, a single-bit toggle is used to number the phases within a grace period. A given phase completes only after each thread’s local snapshot either contains a copy of the phase’s number or indicates the thread is in a quiescent state. If RCU read-side critical sections are finite in duration, one of these two cases must eventually hold for each thread.

Because reader threads snapshot the value of \texttt{rcu\_gp\_ctr} whenever they enter an outermost read-side critical section, explicit tracking of critical-section nesting is required. Nevertheless, the extra read-side overhead is significantly less than a single compare-and-swap operation on most hardware, and a beneficial side effect is that all quiescent states are effectively extended quiescent states. Read-side critical-section nesting is tracked in the lower-order bits (RCU\_NEST\_MASK) of the per-thread \texttt{rcu\_reader.ctr} variable, as shown in Figure 6. The grace-period phase number occupies only a single high-order bit (RCU\_GP\_CTR\_PHASE), so there is ample room to store the nesting level.

The \texttt{rcu\_read\_lock()} function first checks the per-thread nesting level to see if the calling thread was previously in a quiescent state, snapshotting the global \texttt{rcu\_gp\_ctr} grace-period phase number [15] and executing a memory
barrier if it was, and otherwise simply incrementing the nesting level without changing the phase number. The low-order bits of rcu_gp_ctr are permanently set to show a nesting level of 1, so that the snapshot can store both the current phase number and the initial nesting level in a single atomic operation. The memory barrier ensures that the store to rcu_reader.ctr will be ordered before any access in the subsequent RCU read-side critical section. The rcu_read_unlock() function executes a memory barrier and decrements the nesting level. The memory barrier ensures that any access in the prior RCU read-side critical section is ordered before the nesting-level decrement. Even with the memory barriers, both rcu_read_lock() and rcu_read_unlock() are wait-free with maximum overhead smaller than many other synchronization primitives. Because they may be implemented as empty functions, rcu_quiescent_state(), rcu_->thread_offline(), and rcu_thread_online() are omitted.

Figure 7 shows synchronize_rcu() and its two helper functions, update_counter_and_wait() and rcu_gp_ongoing(). The synchronize_rcu() function forces ordering of the caller’s accesses (lines 3 and 9) and waits for two grace-period phases under the protection of rcu_gp_lock, as discussed earlier. The two phases are separated by a barrier() to prevent the compiler from interleaving their accesses, which could result in starvation. The update_counter_and_wait() function is invoked to handle each grace-period phase. This function is similar to its counterpart in Figure 5, the only difference being that the update to rcu_gp_ctr toggles the phase number rather than incrementing a counter. The rcu_gp_ongoing() function is likewise similar to its earlier counterpart; it tests whether the specified snapshot indicates that the corresponding thread is in a non-quiescent state (the nesting level is nonzero) with a phase number different from the current value in rcu_gp_ctr.

To show why this works, let us verify that this two-phase approach properly obeys RCU’s semantics, i.e., that any read-side critical section in progress when synchronize_rcu() begins will terminate before it ends. Suppose thread T is in a read-side critical section. Until the critical section terminates, T’s rcu_reader.ctr will show a nonzero nesting level, and its snapshot of the phase number will not change (since the phase number in rcu_reader.ctr changes only during an outermost rcu_read_lock() call). The invocation of update_counter_and_wait() during one of synchronize_rcu()’s grace-period phases will wait until T’s phase-number snapshot takes on the value 0, whereas the invocation during the other phase will wait until the phase-number snapshot takes on the value 1. Each of the two invocations will also complete if T’s nesting level takes on the value 0. But regardless of how this works out, it is clearly impossible for both phases to end before T’s read-side critical section has terminated. Appendix G presents a semi-formal verification of this reasoning.

A natural question is “Why doesn’t a single grace-period phase suffice?” If synchronize_rcu() used a single phase then it would be essentially the same as the function in Figure 5, and it would be subject to the same overflow problem, exacerbated by the use of what is effectively a single-bit counter. In more detail, the following could occur:

1) Thread T invokes rcu_read_lock(), fetching the value of rcu_gp_ctr, but not yet storing it.
2) Thread U invokes synchronize_rcu(), including invoking update_counter_and_wait(), where it toggles the grace-period phase number in rcu_gp_ctr so that the phase number is now 1.
3) Because no thread is yet in an RCU read-side critical section, thread U completes update_counter_and_wait() and returns to synchronize_rcu(), which returns to its caller since it uses only one phase.
4) Thread T now stores the old value of rcu_gp_ctr, with its phase-number snapshot of 0, and proceeds into its read-side critical section.
5) Thread U invokes synchronize_rcu() once more, again toggling the global grace-period phase number, so that the number is again 0.
6) When Thread U examines Thread T’s rcu_reader.ctr variable, it finds that the phase number in the snapshot matches that of the global variable rcu_gp_ctr. Thread U therefore exits from synchronize_rcu().
7) But Thread T is still in its read-side critical section, in violation of RCU’s semantics.

The extra overhead of a second grace-period phase is not regarded as a serious drawback since it affects only updaters, not readers. The overhead of the read-side memory barriers is more worrisome; the next section shows how it can be
eliminated.

4) Low-Overhead RCU Via Signal Handling: On common multiprocessor hardware, the largest source of read-side overhead for general-purpose RCU is the memory barriers. One novel way to eliminate these barriers is to send POSIX signals from the update-side primitives. An unexpected but quite pleasant surprise is that this approach results in relatively simple read-side primitives. In contrast, those of older versions of the Linux kernel’s preemptible RCU were notoriously complex [16].

The read-side primitives shown in Figure 8 are identical to those in Figure 6, except that lines 9 and 17 replace the memory barriers with compiler directives that suppress code-motion optimizations. The structures, variables, and constants are identical to those in Figures 3 and 6. As with the previous two implementations, both rcu_read_lock() and rcu_read_unlock() are wait-free.

The synchronize_rcu() primitive shown in Figure 9 is similar to that in Figure 7, the only changes being in lines 3–4 and 8–9. Instead of executing a memory barrier local to the current thread, this implementation forces all threads to execute a memory barrier using force_mb_all_threads(), and the two calls to this new function are moved inside the locked region because of the need to iterate over the thread registry, which is protected by rcu_gp_lock. The update_counter_and_wait() and rcu_gp_ongoing() routines are identical to those in Figure 7 and are therefore omitted.

Figure 10 shows the signal-handling functions force_mb_all_threads() and sigurcu_handler() [8]. Of course, these signals must be used carefully to avoid destroying the readers’ wait-free properties, hence the serialization of synchronize_rcu(). With simple batching techniques, concurrent invocations of synchronize_rcu() could share a single RCU grace period.

The force_mb_all_threads() function is invoked from synchronize_rcu(). It ensures a memory barrier is executed on each running thread by sending a POSIX signal to all threads and then waiting for each to respond. As shown in Appendix H, this has the effect of promoting compiler-ordering directives such as barrier() to full memory barriers, while allowing reader threads to avoid the overhead of memory barriers when they are not needed. An initial iteration over all threads sets each need_mb per-thread variable to 1, ensures that this assignment will be seen by the signal handler, and sends a POSIX signal. A second iteration then rescans the threads, waiting until each one has responded by setting its need_mb per-thread variable back to zero [9]. Because some versions of some operating systems can lose signals, a production-quality implementation will resend the signal if a response is not received in a timely fashion. Finally, there is a memory barrier to ensure that the signals have been received and acknowledged before later operations that might otherwise destructively interfere with readers.

The signal handler runs in the context of a reader thread in response to the signal sent in line 8. This sigurcu_handler() function executes a pair of memory barriers enclosing an assignment of its need_mb per-thread variable to zero. The effect is to place a full memory barrier at the

---

1 static inline void rcu_read_lock(void)
2 {
3     unsigned long tmp;
4     tmp = rcu_reader.ctr;
5     if (!!(tmp & RCU_NEST_MASK)) {
6         STORE_SHARED(rcu_reader.ctr, LOAD_SHARED(rcu_gp_ctr));
7         barrier();
8     } else {
9         STORE_SHARED(rcu_reader.ctr, tmp + RCU_NEST_COUNT);
10     }
11     rcu_reader.ctr - RCU_NEST_COUNT);
12 }
13 }
14
15 static inline void rcu_read_unlock(void)
16 {
17     barrier();
18     STORE_SHARED(rcu_reader.ctr, rcu_reader.ctr - RCU_NEST_COUNT);
19     }
20 }

Fig. 8. RCU Read Side Using Signals

1 void synchronize_rcu(void)
2 {
3     mutex_lock(rcu_gp_lock);
4     force_mb_all_threads();
5     update_counter_and_wait();
6     barrier();
7     update_counter_and_wait();
8     force_mb_all_threads();
9     mutex_unlock(rcu_gp_lock);
10 }

Fig. 9. RCU Update Side Using Signals

1 static void force_mb_all_threads(void)
2 {
3     struct rcu_reader *index;
4     list_for_each_entry(index, &registry, node) {
5         STORE_SHARED(index->need_mb, 1);
6         smp_mb();
7         pthread_kill(index->tid, SIGURCU);
8     }
9     list_for_each_entry(index, &registry, node) {
10         while (LOAD_SHARED(index->need_mb))
11             msleep(1);
12         }
13 
14     smp_mb();
15     }
16
17 static void sigurcu_handler(int signo,
18     siginfo_t *siginfo,
19     void *context)
20 {
21     smp_mb();
22     STORE_SHARED(rcu_reader.need_mb, 0);
23     }
24 }

Fig. 10. RCU Signal Handling for Updates
point in the receiver’s code that was interrupted by the signal, preventing the CPU from reordering memory references across that point.

A proof of correctness for this implementation is the subject of another paper [17]. Of course, as with the other two RCU implementations, this implementation’s synchronize_rcu() primitive is blocking. The next section shows a way to provide non-blocking RCU updates.

5) Non-Blocking RCU Updates: Although some algorithms use RCU as a first-class technique, RCU is often used only to defer memory reclamation. In these situations, given sufficient memory, synchronize_rcu() need not block the update itself, just as automatic garbage collectors need not block non-blocking algorithms. The details described here can be used to perform batched RCU callback execution, allowing multiple callbacks to execute after a grace period has passed.

One way of accomplishing this is shown in Figure 11, which implements the asynchronous call_rcu() primitive found in the Linux kernel. The function initializes an RCU callback structure and uses a non-blocking enqueue algorithm [18] to add the callback to the rcu_data list. Given that the call_rcu() function contains but two simple (and therefore wait-free) assignment statements and an invocation of the non-blocking enqueue() function, call_rcu() is clearly non-blocking. Systems providing an atomic swap instruction can implement a wait-free call_rcu() via the wait-free enqueue algorithm used by some queued locks [19].

A separate thread would remove and invoke these callbacks after a grace period has elapsed, by calling the call_rcu_cleanup shown in Figure 11. On each pass through the main loop, the function uses a (possibly blocking) dequeue algorithm to remove all elements from the rcu_data list en masse. If any elements were present, it waits for a grace period to elapse and then invokes all the RCU callbacks dequeued from the list. Finally, line 24 blocks for a short period to allow additional RCU callbacks to be enqueued. The longer line 24 waits, the more RCU callbacks will accumulate on the rcu_data list; this is a classic memory/CPU trade-off, with longer waits allowing more memory to be occupied by RCU callbacks but decreasing the per-callback CPU overhead.

Of course, the use of synchronize_rcu() causes call_rcu_cleanup() to be blocking, so it should be invoked in a separate thread from the updaters. However, if the synchronization mechanism used to coordinate RCU updates is non-blocking then the updater code paths will execute two non-blocking code sequences in succession (the update and call_rcu()), and will therefore themselves be non-blocking.

E. Effects of Updates on Read-Side Performance

This section expands on the results in the printed paper. The RCU read-side performance shown in Figures 12 and 13 (taken from the printed paper) trails off at high update rates. In principle this could be caused either by the overhead of quiescent-state detection on the write side or by cache interference resulting from the data pointer exchanges. To determine the cause, we defined ideal RCU performance to include only the overheads of the grace periods, and compared this ideal performance to that shown in the earlier figures. We generated the ideal RCU workload by removing the memory allocation and pointer exchanges from the update-side, but we kept the rcu_defer() mechanism in order to take into account the overhead of waiting for quiescent states. Figures 14 and 15 present the resulting comparison, clearly
showing that the non-linear read-side performance is caused by the pointer exchanges rather than the grace periods.

F. Verification of Quiescent-State-Based Reclamation RCU

This appendix presents a semi-formal verification that the QSBR implementation satisfies RCU’s grace-period guarantee. Unfortunately it is not possible to prove this outright, owing to the 32-bit wraparound failure discussed in Appendix D2. We will therefore assume that such failures don’t occur.

Theorem: Assuming that threads are never preempted for too long (see below), in any execution of a program using the QSBR implementation, the grace-period guarantee (Formula I in Appendix C1) is satisfied.

Proof: Given QSBR’s implementation, we focus on active segments: the periods between quiescent states. More precisely, an active segment is a sequence of instructions bounded at the start by rcu_quiescent_state(), rcu_thread_online(), or lines 12–15 of synchronize_rcu() in Figure 5; bounded at the end by rcu_quiescent_state(), rcu_thread_offline(), or lines 5–8 of synchronize_rcu() in Figure 5; and containing no other references to rcu_reader_crt. Every read-side critical section is part of an active segment.

Execution of the $k$th active segment in thread $T$ (comprising statements $R_{k,i}$ together with some of the bounding statements) can be represented as a sequence of labelled pseudo-code instructions:

\[
\begin{align*}
\text{Ld}(x_k): & \quad x_k = \text{rcu_gp_ctr} \\
\text{St}(x_k): & \quad \text{rcu_reader.crt} = x_k \\
\text{MB}^2_k: & \quad \text{smp_mb()} \\
\text{MB}^3_k: & \quad \text{rcu_thread_online()} \\
\text{Ld}(y_k): & \quad y_k = (\text{either rcu_gp_ctr or 0}) \\
\text{St}(y_k): & \quad \text{rcu_reader.crt} = y_k
\end{align*}
\]

Here $x_k$ and $y_k$ are intermediate values and \text{rcu_reader.crt} refers to $T$‘s instance of the per-thread rcu_reader structure. The Ld$(y_k)$ line sets $y_k$ to \text{rcu_gp ctr} if the active segment ends with \text{rcu_quiescent_state}() (in which case $y_k$ is $x_{k+1}$, as the call will also mark the beginning of the next active segment); otherwise it sets $y_k$ to 0.

Execution of update_counter_and_wait() is of course serialized by the \text{rcu_gp_lock} mutex. The $n$th occurrence of this routine, together with the statements preceding $(M_{n,i})$ and following it $(D_{n,j})$, can be expressed as:

\[
\begin{align*}
\text{MB}^2_n: & \quad \text{smp_mb()} \\
\text{Ld}(z_n): & \quad z_n = \text{rcu_gp_ctr} + 2 \\
\text{St}(z_n): & \quad \text{rcu_gp_ctr} = z_n \\
\text{As}_n: & \quad \text{assert}(v_n = 0 \text{ or } v_n = z_n) \\
\text{MB}^3_n: & \quad \text{smp_mb()} \\
\text{D}_{n,0}; & \quad \text{D}_{n,1}; \quad \text{D}_{n,2}; \quad \ldots
\end{align*}
\]

Several things are omitted from this summary, including the list_for_each_entry() loop iterations for threads other than $T$ and all iterations of the while loop other than the last (the assertion \text{As}_n holds precisely because this is the last loop iteration). Both here and above, the use of \text{barrier()}, \text{LOAD_SHARED()}, and \text{STORE_SHARED()} primitives forces the compiler to generate the instructions in the order shown. However the hardware is free to reorder them, within the limits imposed by the memory barriers.

We number the grace periods starting from 1, letting $\text{St}(z_0)$ stand for a fictitious instruction initializing $\text{rcu_gp_ctr}$ to 1 before the program starts. In this way each Ld$(x_k)$ is preceded by some St$(z_n)$. Furthermore, because there are no other assignments to $\text{rcu_gp_ctr}$, it is easy to see that for each $n$, $z_n$ is equal to $2n + 1$ truncated to the number of bits in an unsigned long.

Our initial assumption regarding overly-long preemption now amounts to the requirement that not too many grace periods occur between each Ld$(x_k)$ and the following St$(x_k)$. Grace periods $m$ through $n-1$ occur during this interval when Ld$(x_k) \rightarrow \text{St}(z_m)$ and Ld$(y_{n-1}) \rightarrow \text{St}(x_k)$ (recall that “→” indicates that the statement on the left executes prior to that on the right). Under such conditions we therefore require $n - m$ to be sufficiently small that $2(n - m + 1)$ does not overflow an unsigned long and hence $z_{n-1} \neq z_n$.

Let us now verify the grace-period guarantee for a read-side
critical section occurring during thread \( T \)'s active segment \( k \) and for grace period \( n \).

Case 1: \( \text{St}(z_n) \rightarrow \text{Ld}(x_k) \). Since these two instructions both access \( \text{rcu\_gp\_ctr} \), the memory barrier property for \( \text{MB}_n^2 \) and \( \text{MB}_n^0 \) says that \( M_{n,i} \rightarrow R_{k,j} \) for each \( i, j \). Thus Formula 1 in Appendix C1 holds because its left disjunct is true.

Case 2: \( \text{Ld}(v_n) \rightarrow \text{St}(x_k) \). Since these two instructions both access \( \text{rcu\_reader\_ctr} \), the memory barrier property for \( \text{MB}_n^2 \) and \( \text{MB}_n^0 \) says that \( M_{n,i} \rightarrow R_{k,j} \) for each \( i, j \). The rest follows as in Case 1.

Case 3: \( \text{St}(y_k) \rightarrow \text{Ld}(v_n) \). Since these two instructions both access \( \text{rcu\_reader\_ctr} \), the memory barrier property for \( \text{MB}_n^2 \) and \( \text{MB}_n^0 \) says that \( M_{n,i} \rightarrow R_{k,j} \) for each \( i, j \). Thus Formula 1 holds because its right disjunct is true.

Case 4: None of Cases 1–3 above. Since cache coherence guarantees that loads and stores from all threads to a given variable are totally ordered, it follows that \( \text{Ld}(x_k) \rightarrow \text{St}(z_n) \) and \( \text{St}(x_k) \rightarrow \text{Ld}(v_n) \rightarrow \text{St}(y_k) \). We claim that this case cannot occur without violating our assumption about wraparound failures. Indeed, suppose it does occur, and take \( m \) to be the least index for which \( \text{Ld}(x_k) \rightarrow \text{St}(z_m) \). Clearly \( m \leq n \).

Since \( \text{St}(z_{m-1}) \rightarrow \text{Ld}(x_k) \rightarrow \text{St}(z_m) \), \( x_k \) must be equal to \( z_{m-1} \). Similarly, \( v_n \) must be equal to \( x_k \). Since \( z_{m-1} \) cannot be 0, \( \text{As}_v \) implies that \( z_{m-1} = z_n \), and since \( m \leq n \), this is possible only if \( 2(n - m + 1) \) (overflows (and hence \( n > m \)).

Now consider grace period \( n - 1 \). Since \( \text{St}(z_{m-1}) \) precedes \( \text{St}(z_{n-1}) \) we have \( \text{Ld}(x_k) \rightarrow \text{St}(z_{n-1}) \), and since \( \text{Ld}(v_{n-1}) \) precedes \( \text{Ld}(v_n) \) we also have \( \text{Ld}(v_{n-1}) \rightarrow \text{St}(y_k) \). If \( \text{St}(x_k) \rightarrow \text{Ld}(v_{n-1}) \) then active segment \( k \) and grace period \( n - 1 \) would also fall under Case 4, implying that \( z_{m-1} = z_{n-1} \), which is impossible because \( z_{m-1} \neq z_n \). Hence we must have \( \text{Ld}(v_{n-1}) \rightarrow \text{St}(x_k) \). But then \( m \) and \( n \) would violate our requirement on the number of grace periods elapsing between \( \text{Ld}(x_k) \) and \( \text{St}(x_k) \). QED.

### G. Verification of General-Purpose RCU

This appendix presents a semi-formal verification that the general-purpose implementation satisfies RCU’s grace-period guarantee, assuming that read-side critical sections are not nested too deeply.

**Proof:** Using the same notation as in Appendix F, execution of the \( k \)th outermost read-side critical section in thread \( T \) can be represented as follows:

\[ x_{k,0} = \text{rcu\_gp\_ctr} \]

\[ \text{St}(x_{k,0}) : \text{rcu\_reader\_ctr} = x_{k,0} \]

\[ \text{MB}_k^0 : \text{smp\_mb}() \]

\[ \{ \text{R}_{k,0}; R_{k,1}; R_{k,2}; \ldots \} \]

\[ \text{St}(x_{k,i}) : \text{rcu\_reader\_ctr} = x_{k,i}; \text{RCU\_NEST\_COUNT} - 1 \]

\[ \text{MB}_k^1 : \text{smp\_mb}() \]

\[ \text{y}_k = \text{rcu\_reader\_ctr} - \text{RCU\_NEST\_COUNT} \]

\[ \text{St}(y_k) : \text{rcu\_reader\_ctr} = y_k \]

Here \( x_{k,0} \) is the value read by \( \text{LOAD\_SHARED}() \) in the outermost \( \text{rcu\_read\_lock}() \), \( x_{k,i} \) for \( i > 0 \) corresponds to the \( i \)th nested call by thread \( T \) to \( \text{rcu\_read\_lock}() \) or \( \text{rcu\_read\_unlock}() \) in time order (the ‘[...]' notation is intended to express that these calls are interspersed among the \( R_{k,i} \) statements), and \( y_k \) is the value in the \( \text{STORE\_SHARED}() \) call in the \( \text{rcu\_read\_unlock}() \) that ends the critical section. The memory barriers are present because this is an outermost read-side critical section.

The \( n \)th occurrence of \( \text{synchronize\_rcu}() \), together with the statements preceding and following it, can similarly be expressed as:

\[ \text{MB}_n^2 : \text{smp\_mb}() \]

\[ \text{MB}_n^0 : \text{rcu\_gp\_ctr} = \text{RCU\_GP\_CTR\_PHASE} \]

\[ \text{ld}(v_n)^0 = \text{rcu\_reader\_ctr} \]

\[ \text{as}_n^0 : \text{assert}(v_n^0\text{'}\text{s nesting level is 0 or its phase number agrees with rcu\_gp\_ctr}) \]

\[ \text{MB}_n^2 : \text{smp\_mb}() \]

\[ D_{n,0}; D_{n,1}; D_{n,2}; \ldots \]

As before, the assertions hold because these statements are from the last iteration of the while loop for thread \( T \). We can now verify the grace-period guarantee for \( T \)'s read-side critical section \( k \) and for grace period \( n \).

Case 1: \( \text{Ld}(v_n^m) \rightarrow \text{St}(x_{k,0}) \), \( m = 0 \) or 1. Since these instructions all access \( \text{rcu\_reader\_ctr} \), the memory barrier property for \( \text{MB}_n^0 \) and \( \text{MB}_n^1 \) says that \( M_{n,i} \rightarrow R_{k,j} \) for each \( i, j \). Thus Formula 1 in Appendix C1 holds because its left disjunct is true.

Case 2: \( \text{St}(y_k) \rightarrow \text{Ld}(v_n^m) \), \( m = 0 \) or 1. Then the memory barrier property for \( \text{MB}_n^0 \) and \( \text{MB}_n^1 \) says that \( R_{k,i} \rightarrow D_{n,j} \) for each \( i, j \). Thus Formula 1 holds because its right disjunct is true.

Case 3: Neither of Cases 1–2 above. For each \( m \) we must have \( \text{St}(x_{k,0}) \rightarrow \text{Ld}(v_n^m) \rightarrow \text{St}(y_k) \); therefore \( v_n^0 \) and \( v_n^1 \) must be equal to \( x_{k,i} \) for some values of \( i \geq 0 \). We are assuming that the maximum nesting level of read-side critical sections does not exceed the 16-bit capacity of \( \text{RCU\_NEST\_MASK} \); therefore each \( x_{k,i} \) has a nonzero nesting level and has the same phase number as \( x_{k,0} \), and the same must be true of \( v_n^0 \) and \( v_n^1 \). However the phase number of \( \text{rcu\_gp\_ctr} \) is different in \( \text{As}_n^0 \) and \( \text{As}_n^1 \), thanks to \( \text{To}_n^1 \). Hence \( \text{As}_n^0 \) and \( \text{As}_n^1 \) cannot both hold, implying that this case can never arise. QED.

### H. Verification of Barrier Promotion Using Signals

This appendix discusses how the signal-based RCU implementation is able to “promote” compiler barriers to full-fledged memory barriers. A more accurate, if less dramatic, statement is that the combination of \( \text{barrier}() \) and \( \text{force\_mb\_all\_threads}() \) obeys a strong form of the fundamental ordering property of memory barriers. Namely, if one thread executes the statements
A0; A1; A2; ...; barrier(); B0; B1; B2; ...; and another thread executes the statements

C0; C1; C2; ...; force_mb_all_threads();
D0; D1; D2; ...

then either Ai → Dj (all i, j) or Ci → Bj (all i, j).
To see why, consider that the pthread_kill() call in
force_mb_all_threads() forces the first thread to invoke sigrcu_handler() at some place in its instruction stream, either before all the Bj or after all the Ai (although barrier() does not generate any executable code, it does force the compiler to emit all the object code for the Ai instructions before any of the Bj object code). Suppose sigrcu_handler() is called after all the Ai. Then the first thread actually executes

A0; A1; A2; ...; smp_mb();
STORE_SHARED(rcu_reader.need_mb, 0);

Since the second thread executes

LOAD_SHARED(index->need_mb); ...;
smp_mb(); D0; D1; D2; ...

in its last loop iteration for the first thread and the following statements, and since the LOAD_SHARED() sees the value stored by the STORE_SHARED(), it follows that Ai → Dj for all i, j. The case where sigrcu_handler() runs before all the Bj can be analyzed similarly.

REFERENCES


